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Carl-Zeiss Lecture 2

IPHT Jena

Resonance Raman Spectroscopy; Theory and Experiment

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Landmarks of Raman Spectroscopy (HH view)

Kramers-Heisenberg-Dirac Dispersion Formula

Placzek Polarizability Theory

Albrecht Vibronic Theory

Resonance Raman Spectroscopy

Time-resolved Raman Spectroscopy

(Non-linear Raman, SERS, Raman Microspectroscopy, still moving)

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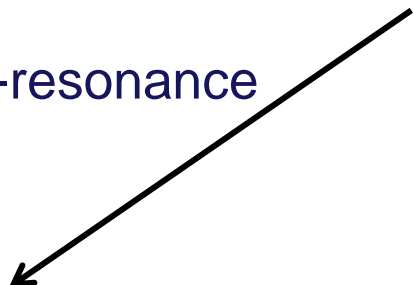
Raman microspectroscopy of Living Cells

Theoretical Framework of Raman Spectroscopy

K-H-D Dispersion Formula



Off-resonance



Placzek Polarizability Theory

Selection rule

$$\left(\frac{\partial \alpha_{\rho\sigma}}{\partial Q_k} \right)_0 \neq 0, \quad \Delta v = 1$$

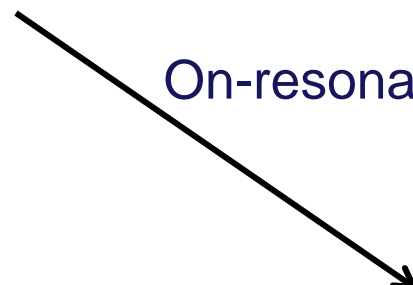
Polarization rule

Totally symmetric mode: $0 \leq \rho < 0.75$

Non-totally symmetric mode: $\rho = 0.75$



On-resonance



Albrecht Vibronic Theory

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Theory of Raman Scattering (1)

Kramers-Heisenberg-Dirac dispersion formula

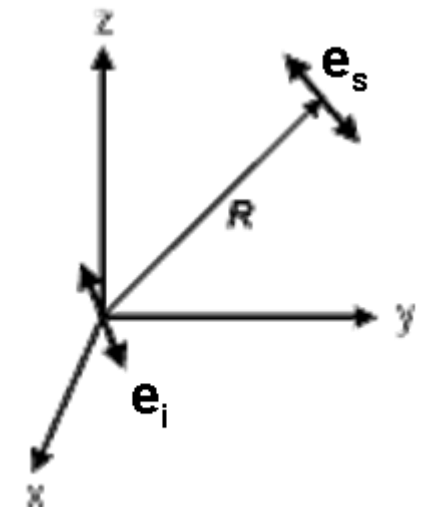
P. A. M. Dirac, Principle of Quantum Mechanics



PAM Dirac
(1902-1984)

$$F_s R^2 = \frac{\omega_s^3 \omega_i}{c^4} |e_s \alpha e_i|^2 F_i$$

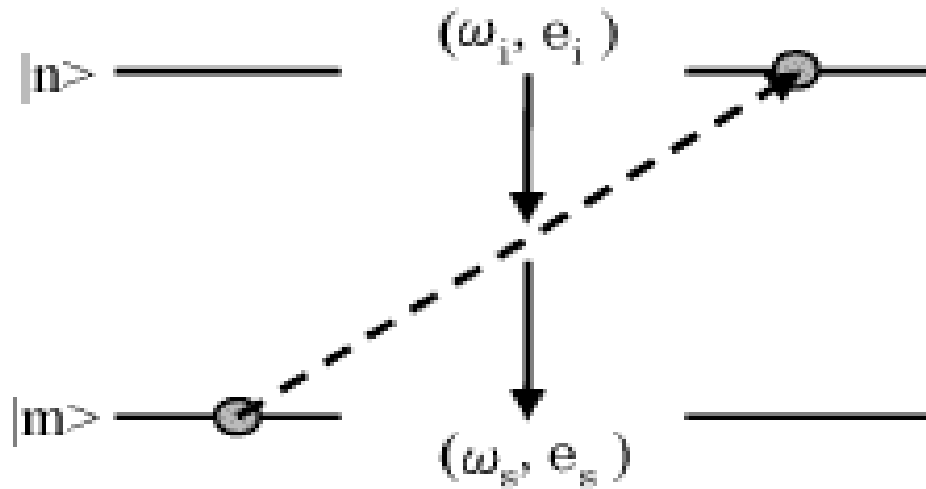
$$\alpha_{\rho\sigma} = \sum_{e \neq m, n} \left\{ \frac{\langle m | D_\sigma | e \rangle \langle e | D_\rho | n \rangle}{E_e - E_m - E_i - i\Gamma_e} + \frac{\langle m | D_\rho | e \rangle \langle e | D_\sigma | n \rangle}{E_e - E_n + E_i + i\Gamma_e} \right\}$$



Quantum Theory of Raman Scattering

The initial and final states of Raman scattering

In the quantum theory of Raman scattering, we calculate the probability for an optical process in which an incident photon with angular frequency ω_i and polarization vector \mathbf{e}_i is annihilated and a new scattered photon with ω_s and \mathbf{e}_s is created with a concomitant molecular transition from the initial state $|m\rangle$ to the final state $|n\rangle$.



The photon number state is expressed as $|n_i, n_s\rangle$, where n_i stands for the number of photon with ω_i and \mathbf{e}_i , n_s that for ω_s and \mathbf{e}_s . The initial state $|i\rangle$ and the final state $|f\rangle$ of Raman scattering are expressed as the products of the photon and the molecular states as;

$$|i\rangle = |n_i, n_s\rangle |m\rangle$$

$$|f\rangle = |n_i - 1, n_s + 1\rangle |n\rangle$$

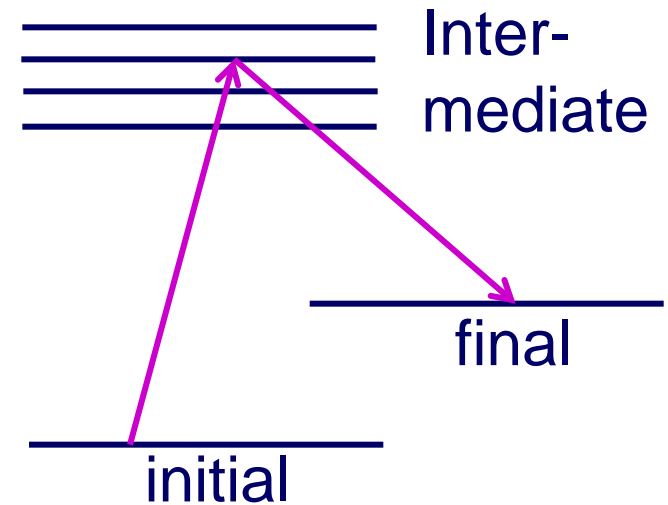
The second-order perturbation theory

$$H_0 |n^{(0)}\rangle = E_n^{(0)} |n^{(0)}\rangle \quad , \quad n = 1, 2, 3, \dots$$

$$H = H_0 + \lambda V$$

$$|n\rangle = |n^{(0)}\rangle + \lambda |n^{(1)}\rangle + \lambda^2 |n^{(2)}\rangle + \dots$$

$$\begin{aligned} (H_0 + \lambda V) (|n^{(0)}\rangle + \lambda |n^{(1)}\rangle + \dots) \\ = \left(E_n^{(0)} + \lambda E_n^{(1)} + \lambda^2 E_n^{(2)} + \dots \right) (|n^{(0)}\rangle + \lambda |n^{(1)}\rangle + \dots) \end{aligned}$$



$$\begin{aligned} |n\rangle = & |n^{(0)}\rangle + \lambda \sum_{k \neq n} |k^{(0)}\rangle \frac{\langle k^{(0)} | V | n^{(0)} \rangle}{E_n^{(0)} - E_k^{(0)}} + \lambda^2 \sum_{k \neq n} \sum_{\ell \neq n} |k^{(0)}\rangle \frac{\langle k^{(0)} | V | \ell^{(0)} \rangle \langle \ell^{(0)} | V | n^{(0)} \rangle}{(E_n^{(0)} - E_k^{(0)}) (E_n^{(0)} - E_\ell^{(0)})} \\ & - \lambda^2 \sum_{k \neq n} |k^{(0)}\rangle \frac{\langle n^{(0)} | V | n^{(0)} \rangle \langle k^{(0)} | V | n^{(0)} \rangle}{(E_n^{(0)} - E_k^{(0)})^2} - \frac{1}{2} \lambda^2 |n^{(0)}\rangle \sum_{k \neq n} \frac{\langle n^{(0)} | V | k^{(0)} \rangle \langle k^{(0)} | V | n^{(0)} \rangle}{(E_n^{(0)} - E_k^{(0)})^2} + O(\lambda^3). \end{aligned}$$

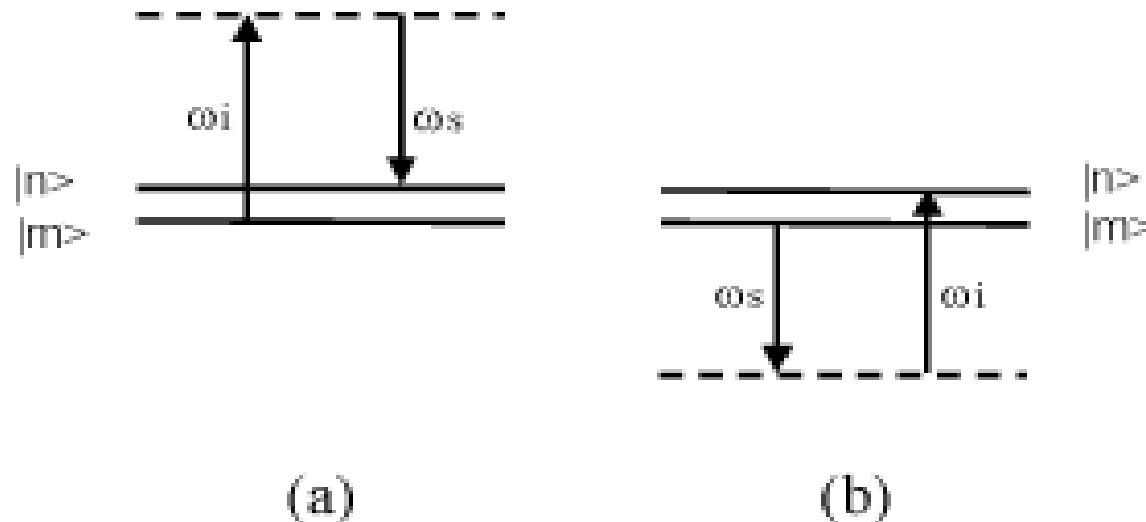
The intermediate states of Raman scattering

The Raman scattering process is obtained as a second order perturbation of the light-matter interaction. There are two kinds of intermediate states that can combine the initial and final states by a one-photon transition induced by a perturbation μE .

$$|v_1\rangle = |n_i - 1, n_s\rangle |e\rangle$$

$$|v_2\rangle = |n_i, n_s + 1\rangle |e\rangle$$

$|v_1\rangle$ corresponds to the state in which an incident photon is annihilated with a molecular transition from $|m\rangle$ to $|e\rangle$ (figure-a, absorption resonance) and $|v_2\rangle$ to that in which one scattered photon is created with $|m\rangle$ to $|e\rangle$ (figure-b, emission resonance).



The contribution of the second intermediate state is characteristic of Raman scattering that distinguishes Raman scattering from fluorescence.

Kramers-Heisenberg-Dirac dispersion formula

In the quantum theory of Raman scattering, it is convenient to use photon flux F in stead of intensity I , $I = h\omega C/2\pi$, where $h\omega/2\pi$ is the photon energy. F indicates the number of photons transmitted per unit time through unit area. The second order perturbation theory gives the following formula that connects the scattered photon number per unit time $F_s R^2$ and the incident photon flux F_i .

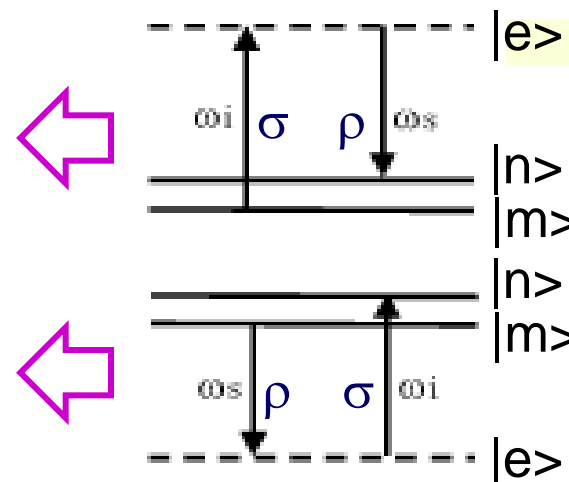
$$|v_1\rangle = |n_i - 1, n_s\rangle |e\rangle \text{ with } E_{v_1} - E_m = -\hbar\omega_i + E_e - E_m = E_e - E_m - E_i$$

$$|v_2\rangle = |n_i, n_s + 1\rangle |e\rangle \text{ with } E_{v_2} - E_m = \hbar\omega_s + E_e - E_m = E_e - E_m - E_s = E_e - E_n + E_i$$

$$F_s R^2 = \frac{\omega_s^3 \omega_i}{c^4} |e_s \alpha e_i|^2 F_i$$

$$a_{\rho\sigma} = \sum_{e \neq m, n} \left\{ \frac{\langle m | D_\sigma | e \rangle \langle e | D_\rho | n \rangle}{E_e - E_m - E_i - i\Gamma_e} \right.$$

$$\left. + \frac{\langle m | D_\rho | e \rangle \langle e | D_\sigma | n \rangle}{E_e - E_n + E_i + i\Gamma_e} \right\}$$



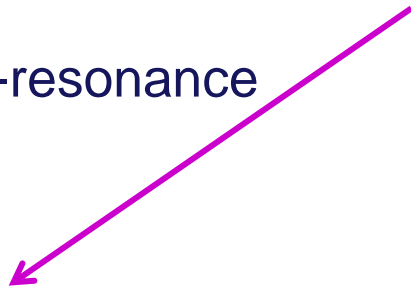
Here, e_i and e_s are the unit polarization vectors of the incident and scattered photons, $a_{\rho\sigma}$ is the Raman scattering tensor with σ and ρ being (x,y,z), and D_σ and D_ρ are the $\rho\sigma$ component of the electric dipole moment.

Theoretical Framework of Raman Spectroscopy

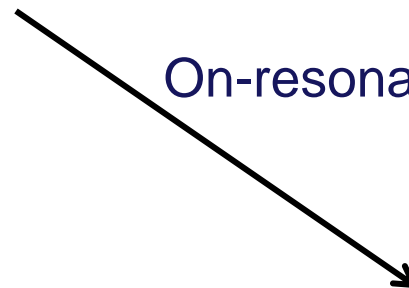
K-H-D Dispersion Formula



Off-resonance



On-resonance



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Selection rule

$$\left(\frac{\partial \alpha_{\rho\sigma}}{\partial Q_k} \right)_0 \neq 0, \quad \Delta v = 1$$

Polarization rule

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Non-totally symmetric mode: $\rho = 0.75$

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Placzek's polarizability theory of off-resonance Raman scattering

By introducing an adiabatic approximation, $|m\rangle = |g\rangle|i\rangle$, $|n\rangle = |g\rangle|f\rangle$, $|e\rangle = |e\rangle|v\rangle$, we obtain the formula for vibrational Raman scattering.

$$\alpha_{\rho\sigma} = \langle i | \langle g | \sum_{e \neq g} \sum_v \left\{ \frac{[g | D_\sigma | e] | v \rangle \langle v | [e | D_\rho | g]}{E_{ev} - E_{gi} - E_i - i\Gamma_e} + \frac{[g | D_\rho | e] | v \rangle \langle v | [e | D_\sigma | g]}{E_{ev} - E_{gf} + E_i + i\Gamma_e} \right\} | g \rangle | f \rangle$$

In off-resonance Raman scattering, $E_{ev} - E_{gi} \gg E_i$ and therefore $E_{ev} - E_{gi} - E_i$ is much larger than the vibrational energies. Then $E_{ev} - E_{gi} - E_i + i\Gamma \sim E_e - E_g - E_i$ holds with a good approximation. Then the closure property $\sum |v\rangle \langle v| = 1$ simplifies the KHD formula to the following form.

$$\alpha_{\rho\sigma} \equiv \langle i | \alpha_{\rho\sigma} | f \rangle$$

$$\alpha_{\rho\sigma} = \sum_{e \neq g} \left\{ \frac{[g | D_\sigma | e][e | D_\rho | g]}{E_e - E_g - E_i} + \frac{[g | D_\rho | e][e | D_\sigma | g]}{E_e - E_g + E_i} \right\}$$

The Raman scattering tensor component $a_{\rho\sigma}$ is approximately given by the vibrational matrix element of the polarizability tensor component $\alpha_{\rho\sigma}$ (Placzek polarizability theory).

Selection rule for off-resonance Raman scattering

The initial vibrational state $|i\rangle$ and the final vibrational state $|f\rangle$ are expressed as the products of vibrational states,

$$|i\rangle = \prod |v_{ki}\rangle \quad (12), \quad |f\rangle = \prod |v_{kf}\rangle, \quad (13)$$

where v_{ki} and v_{kf} are the vibrational quantum numbers of the k -th vibrational mode in the initial and final states.

The polarizability component $\alpha_{\rho\sigma}$ is expanded into a power series of normal coordinates Q_k .

$$\alpha_{\rho\sigma} = (\alpha_0)_{\rho\sigma} + \sum_k \left(\frac{\partial \alpha_{\rho\sigma}}{\partial Q_k} \right)_0 Q_k \quad (14)$$

Under a harmonic approximation, the vibrational matrix element of the polarizability component is given in the following form.

$$\langle i | Q_k | f \rangle \propto \delta_{v_{ki}, v_{kf} \pm 1} \prod_{l \neq k} \delta_{v_{li}, v_{lf}} \quad (15)$$

We finally obtain the selection rule of off-resonance Raman scattering.

$$\left(\frac{\partial \alpha_{\rho\sigma}}{\partial Q_k} \right)_0 \neq 0 \quad (16) \quad \text{and} \quad \Delta v_k = v_{kf} - v_{ki} = \pm 1 \quad (17)$$

Theory of Raman Scattering (2)

Polarizability Theory of Vibrational Raman Scattering

1) Off-resonance condition, 2) Non-degenerate condition

$$\alpha_{\rho\sigma} \equiv \langle i | \alpha_{\rho\sigma} | f \rangle$$

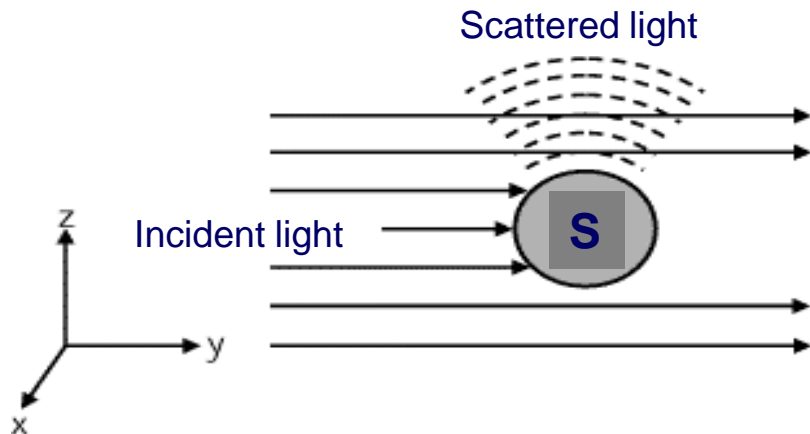
$$\alpha_{\rho\sigma} = \sum_{e \neq g} \left\{ \frac{[g | D_\sigma | e][e | D_\rho | g]}{E_e - E_g - E_i} + \frac{[g | D_\rho | e][e | D_\sigma | g]}{E_e - E_g + E_i} \right\}$$

Selection rule

$$\left(\frac{\partial \alpha_{\rho\sigma}}{\partial Q_k} \right)_0 \neq 0, \quad \Delta v = \pm 1$$

Depolarization ratio $\rho = I_\perp / I_\parallel = I_y / I_x =$

$$\frac{3G_s + 5G_a}{10G_0 + 4G_s}$$



$$a_{\rho\sigma} = a^0_{\rho\sigma} + a^a_{\rho\sigma} + a^s_{\rho\sigma}$$

$$G_0 = \sum (a^0_{\rho\sigma})^2, \quad G_a = \sum (a^a_{\rho\sigma})^2, \quad G_s = \sum (a^s_{\rho\sigma})^2$$

Totally symmetric mode:

$$G_0 \neq 0, \quad G_a = 0, \quad G_s \neq 0 \quad 0 \leq \rho < 0.75$$

Non-totally symmetric mode:

$$G_0 = 0, \quad G_a = 0, \quad G_s \neq 0 \quad \rho = 0.75$$



G. Placzek (1905-1955)

Depolarized Totally-symmetric Raman Band?

Molecule: 1,2-Dichloroethane $\text{CH}_2\text{ClCH}_2\text{Cl}$ (trans form)
 Symmetry C_{2h} Symmetry number $\sigma = 2$

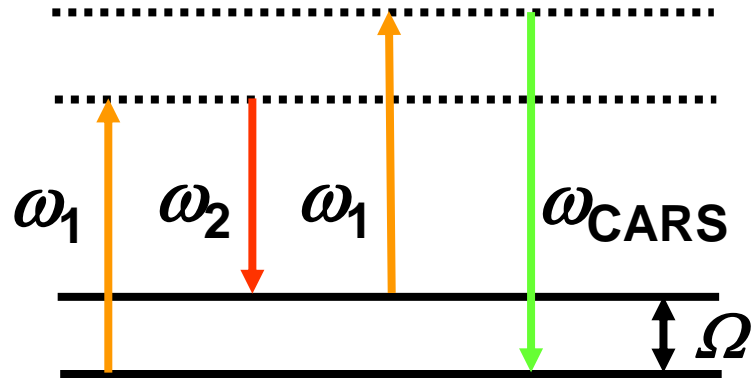
No. 160

Sym. species	No.	Approximate type of mode	Selected value of frequency	Infrared	Raman	Comments
				cm^{-1} (Gas)	cm^{-1} (Liquid)	
a_g	ν_1	CH_2 s-stretch.....	2957 D	ia	2957 (10) p	
	ν_2	CH_2 scis.....	1445 C	ia	1445 (4b) dp	
	ν_3	CH_2 wag.....	1304 C	ia	1304 (6) p	
	ν_4	CC stretch.....	1052 C	ia	1052 (4) p	
	ν_5	CCl stretch.....	754 C	ia	754 (10b) p	
	ν_6	CCCl deform.....	300 C	ia	300 (8) p	
a_u	ν_7	CH_2 a-stretch.....	3005 D	3005 W (liquid)	ia	SF (gauche ν_1 , gauche ν_{11}).
	ν_8	CH_2 twist.....	1123 B	1122.5 W	ia	
	ν_9	CH_2 rock.....	773 B	772.5 M	ia	
b_g	ν_{10}	Torsion.....	123 C	123 M	ia	
	ν_{11}	CH_2 a-stretch.....	3005 D	ia	3005 (8b) dp	
	ν_{12}	CH_2 twist.....	1264 C	ia	1264 (3) dp	
b_u	ν_{13}	CH_2 rock.....	989 C	ia	989 (2) p	
	ν_{14}	CH_2 s-stretch.....	2983 C	2983.3 M	ia	
	ν_{15}	CH_2 scis.....	1461 A	1460.6 S	ia	
	ν_{16}	CH_2 wag.....	1232 B	1232.3 S	ia	
	ν_{17}	CCl stretch.....	728 C	728.3 VS	ia	
	ν_{18}	CCCl deform.....	222 C	222.3 W	ia	

Polarization-resolved CARS Spectroscopy

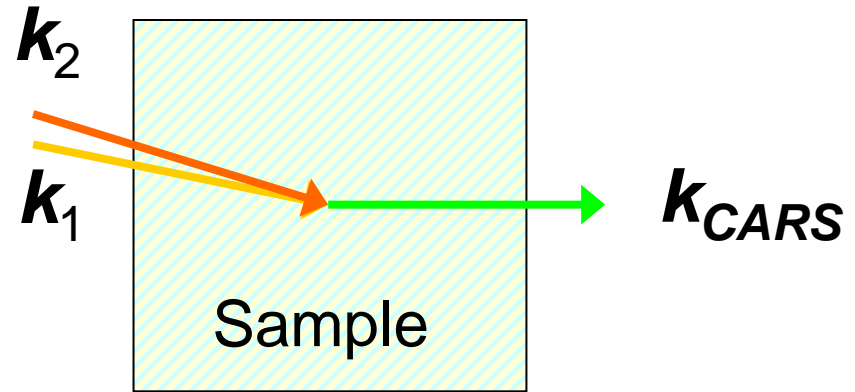
Energy conservation:

$$\omega_{\text{CARS}} = 2\omega_1 - \omega_2 = \omega_1 + \Omega$$

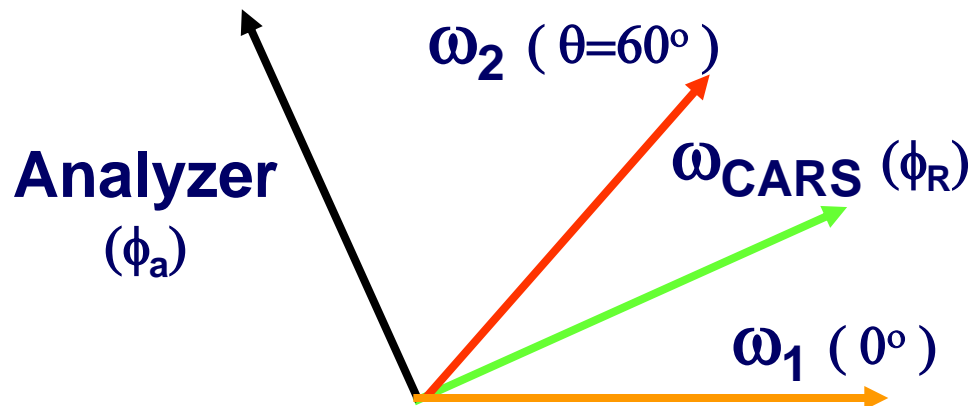


Momentum conservation:

$$\mathbf{k} = 2\mathbf{k}_1 - \mathbf{k}_2$$



Polarization rule: $\tan\phi_R = \rho \tan\theta$ (ρ ; Raman depolarization ratio)



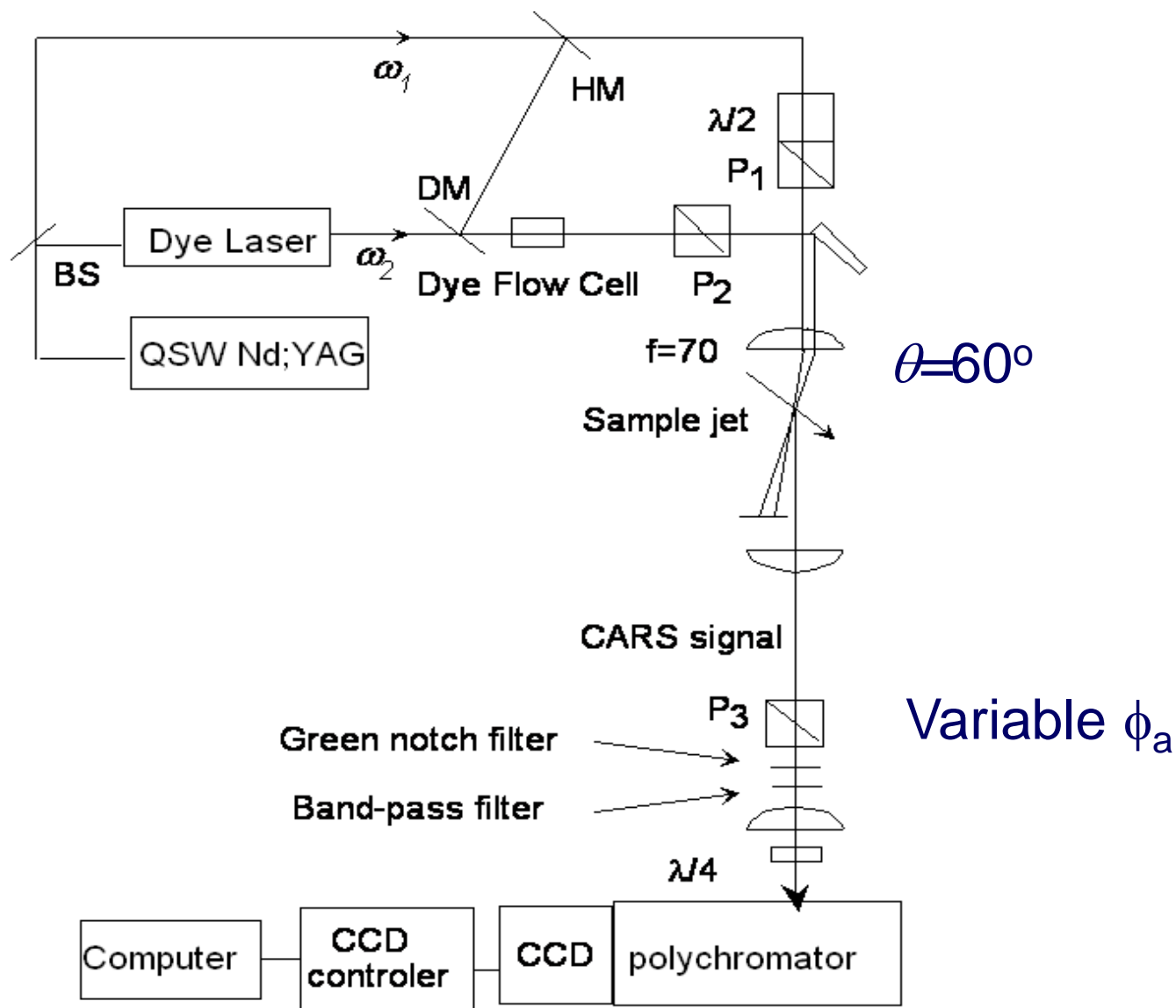
p: $\rho < 0.75$

Totally symmetric mode

dp: $\rho = 0.75$

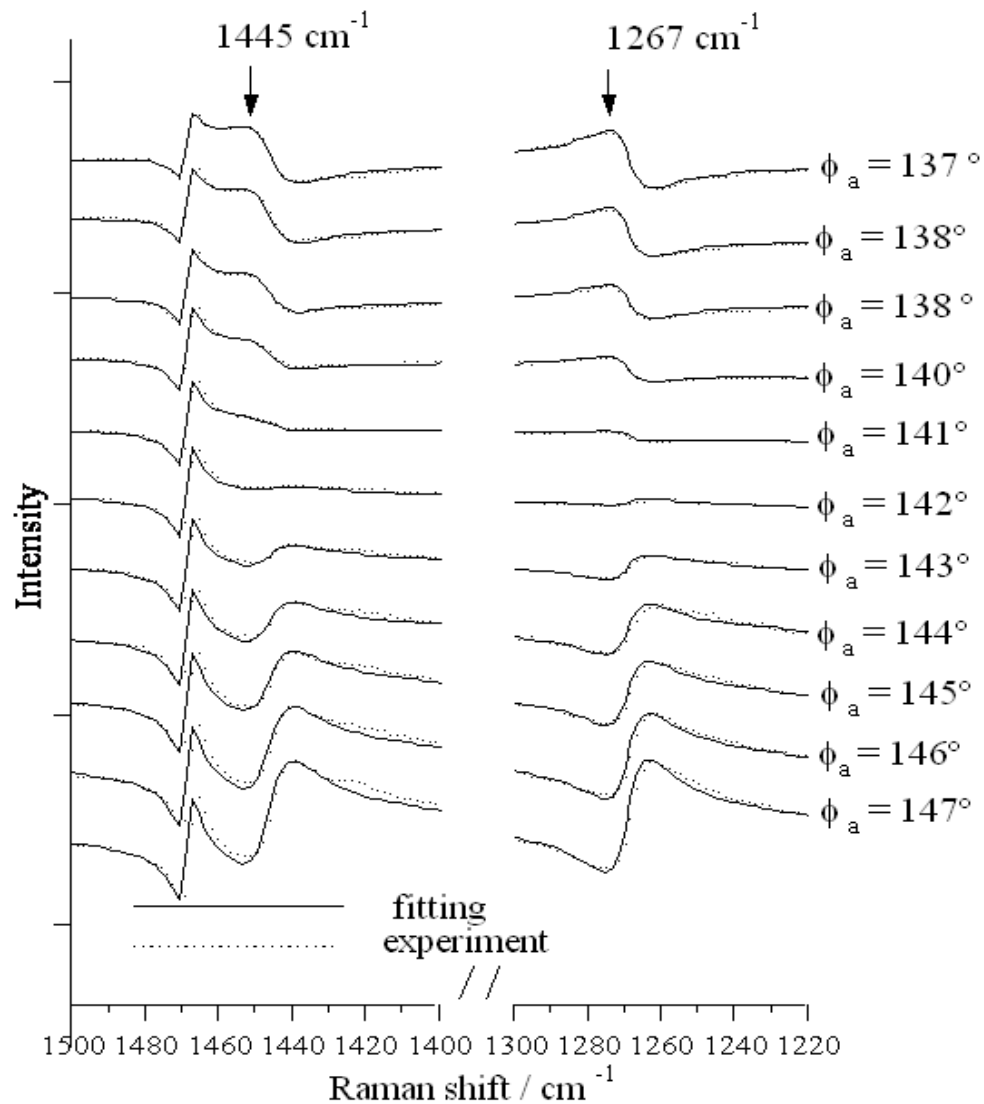
Non-totally symmetric mode

Polarization-resolved CARS Spectroscopy

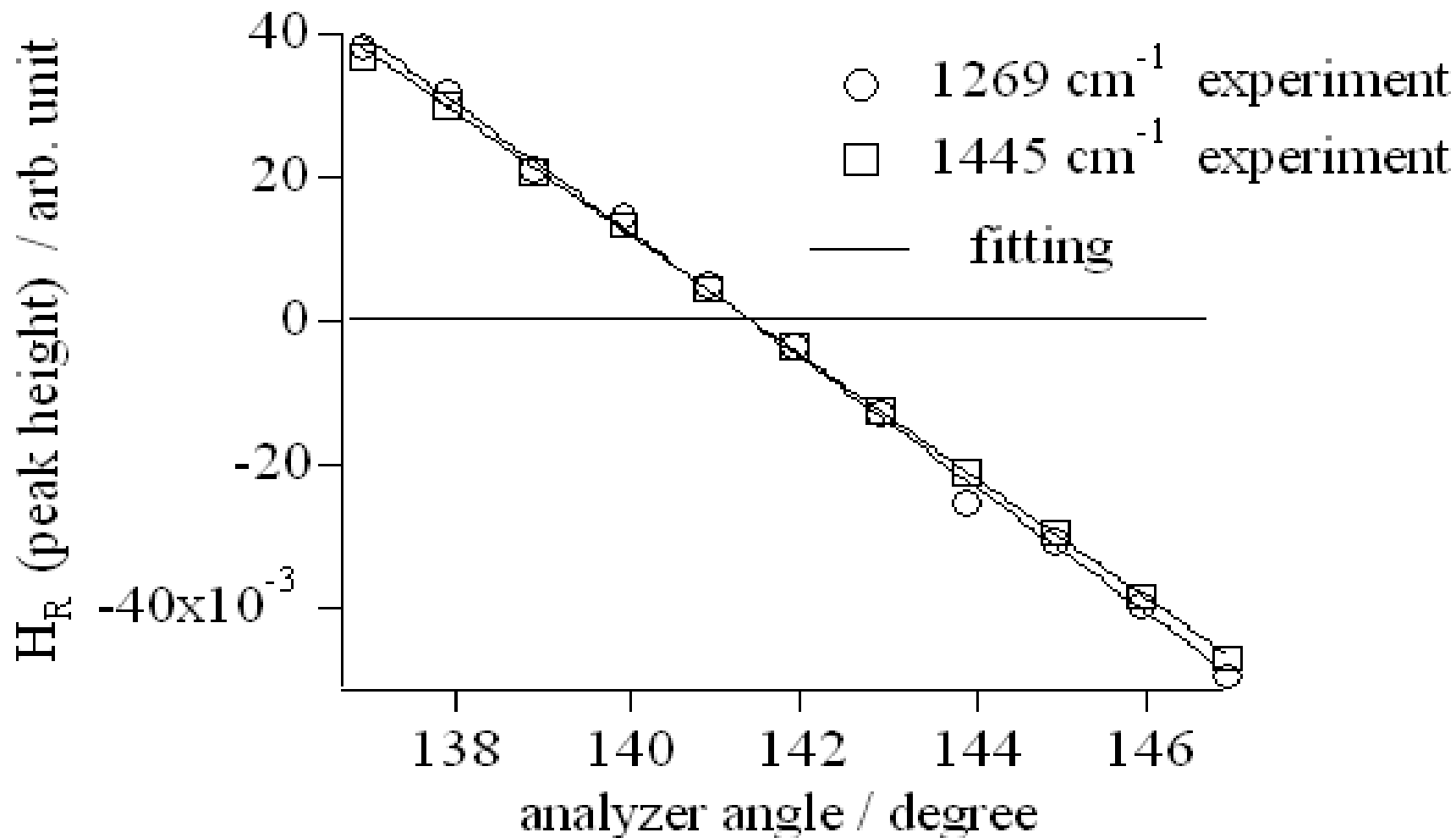


Polarization-resolved CARS Spectra of Liquid Cyclohexane

$$\mathbf{I}_{\text{CARS}} = \left(A_{NR} + \sum_R \frac{H_R G_R}{\omega_R - (\omega_1 - \omega_2) - iG_R} \right)^2$$

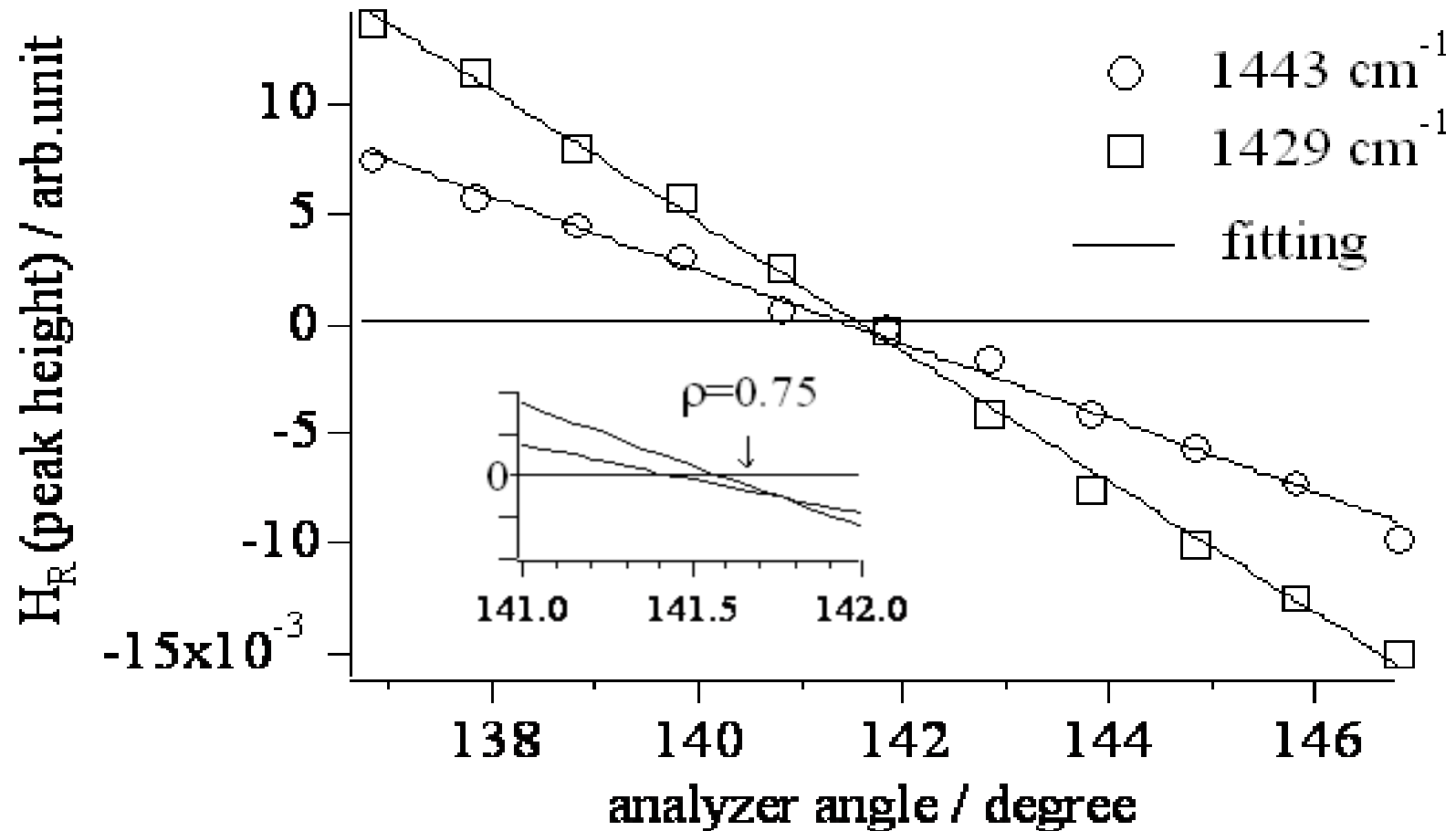


Depolarization Ratios of Two e_g Bands of Cyclohexane



CH ₂ twist	(e_g)	1267 cm^{-1}	0.749 ± 0.002
CH ₂ scissors	(e_g)	1445 cm^{-1}	0.750 ± 0.002

Depolarization Ratios of Two Totally-symmetric Bands of 1,2-dichloroethane



<i>gauche</i> CH ₂ scissors (a)	1429 cm^{-1}	0.746 ± 0.003
<i>trans</i> CH ₂ scissors (a _g)	1443 cm^{-1}	0.742 ± 0.003

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Resonance Raman scattering

RESONANCE RAMAN SPECTROSCOPIC STUDY ON IODINE IN VARIOUS ORGANIC SOLVENTS: SPECTROSCOPIC CONSTANTS AND HALFBAND WIDTHS OF THE I₂ VIBRATION* **

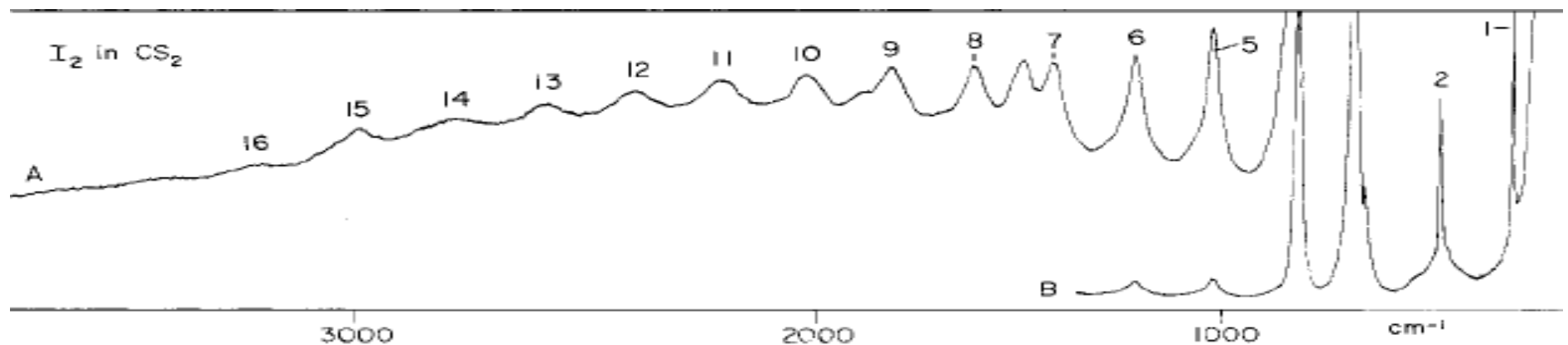
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and

H. J. BERNSTEIN

Division of Chemistry, National Research Council of Canada, Ottawa, Ontario, Canada

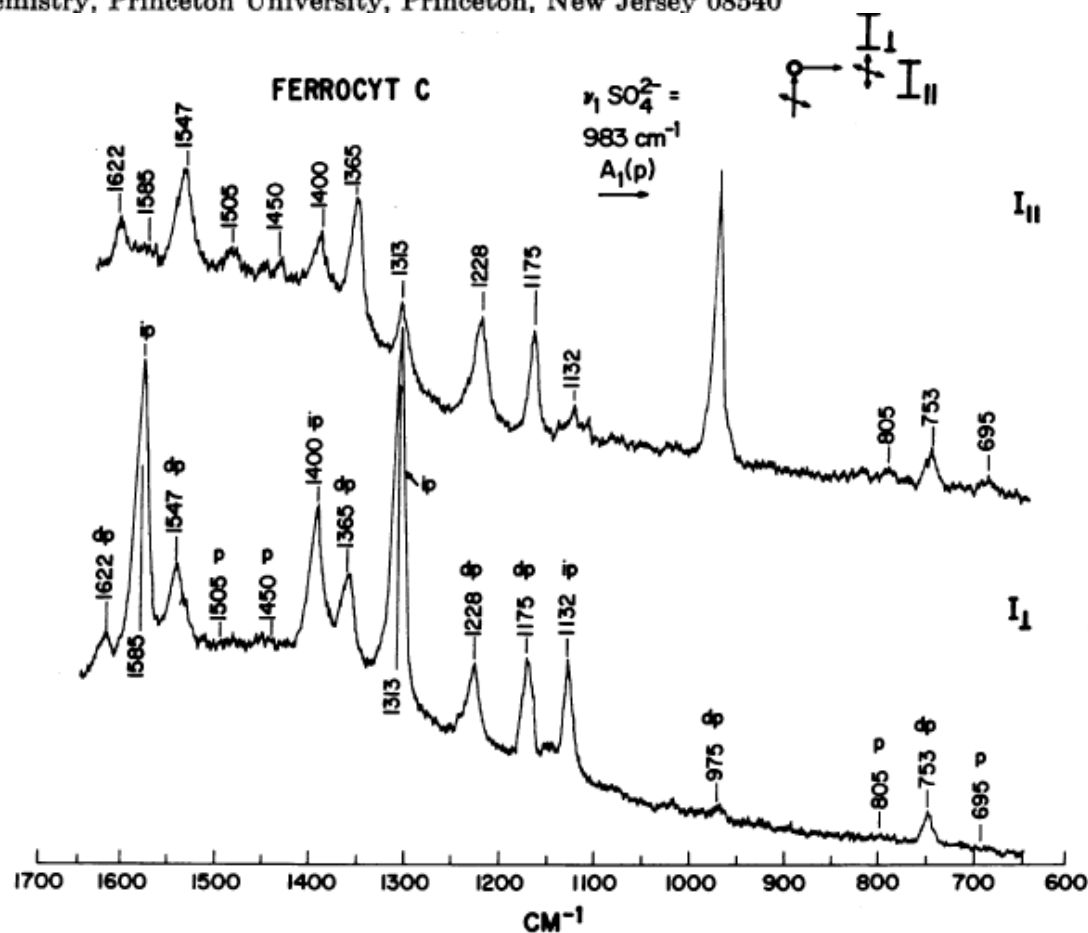


Resonance Raman Spectra of Hemoglobin and Cytochrome c: Inverse Polarization and Vibronic Scattering

(scattering tensor/porphyrin fluorescence)

THOMAS G. SPIRO AND THOMAS C. STREKAS

Department of Chemistry, Princeton University, Princeton, New Jersey 08540

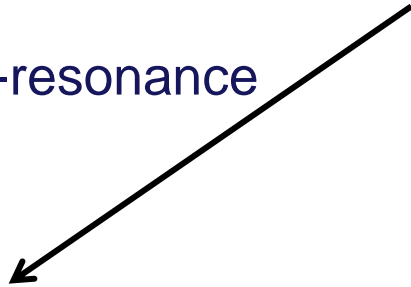


Theoretical Framework of Raman Spectroscopy

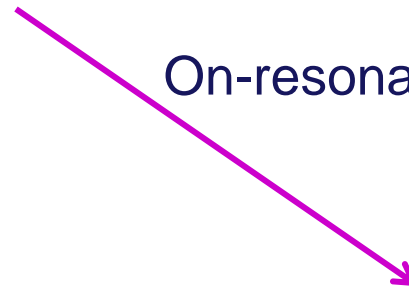
K-H-D Dispersion Formula



Off-resonance



On-resonance



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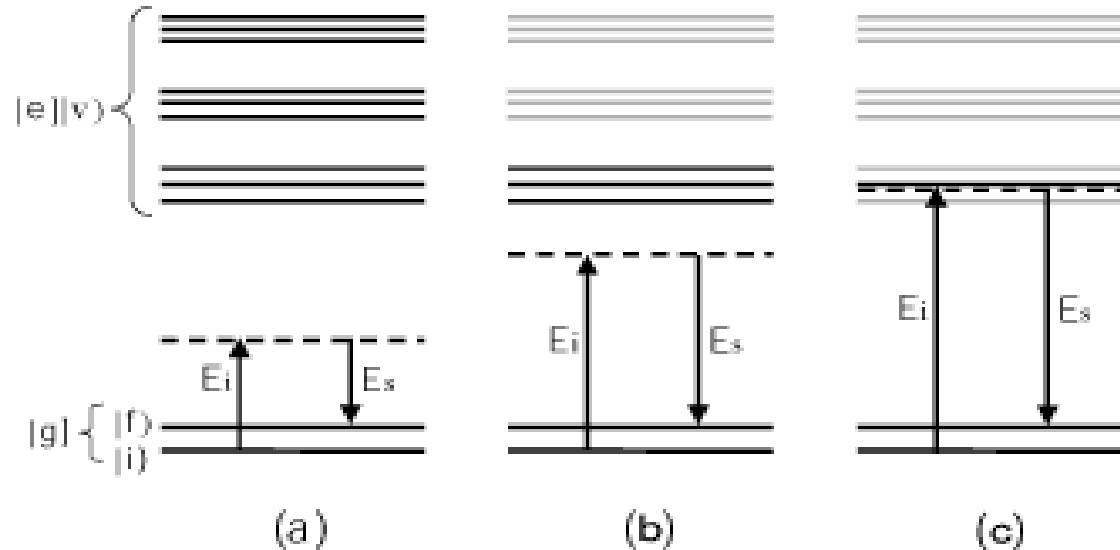
Vibrational Raman scattering and electronic resonance

In vibrational Raman scattering in the ground electronic state, the initial, final and intermediate states are expressed as the products of the electronic and vibrational parts as,

$$|m\rangle = |g\rangle|i\rangle$$

$$|n\rangle = |g\rangle|f\rangle$$

$$|e\rangle = |e\rangle|v\rangle$$



where $| \]$ stands for electronic state and $| \)$ for vibrational state; $|g\rangle$ is the ground electronic state and $|e\rangle$ the excited electronic state(s), and $|i\rangle$, $|f\rangle$, $|v\rangle$ are the initial, final and intermediate vibrational states, respectively.

In off-resonance Raman scattering (a), $E_{ev} - E_{gi} \gg E_i$ and therefore many excited electronic states $\sum |e\rangle|v\rangle$ contribute (virtual intermediate states). In pre-resonance Raman scattering, E_i become close to $E_{ev} - E_{gi}$ and the vibrational states of the lowest excited electronic state $|e\rangle|v\rangle$ play the role of intermediate states. In rigorous resonance Raman scattering, $E_{ev} - E_{gi} \sim E_i$ and one particular vibronic state $|e\rangle|v\rangle$ dominates the scattering process.

For resonance Raman scattering, we need to take explicitly the vibronic nature of the intermediate states. We write the molecular Hamiltonian with three terms, electronic, vibrational and vibronic terms..

$$H_{\text{mol}} = H_{\text{mol}}^{\text{e}} + H_{\text{mol}}^{\text{v}} + H_{\text{mol}}^{\text{ev}} \quad (41)$$

We treat $H_{\text{mol}}^{\text{ev}}$ as a perturbation to $H_{\text{mol}}^{\text{e}}$ and $H_{\text{mol}}^{\text{v}}$. We consider three zero-order electronic states, ground electronic state $|g_0\rangle$, the resonant excited electronic state $|e_0\rangle$ and another excited electronic state $|s_0\rangle$. They satisfy the following equations.

$$H_{\text{mol}}^{\text{e}}|g_0\rangle = E_g^0|g_0\rangle \quad (42)$$

$$H_{\text{mol}}^{\text{e}}|e_0\rangle = E_e^0|e_0\rangle \quad (43)$$

$$H_{\text{mol}}^{\text{e}}|s_0\rangle = E_s^0|s_0\rangle \quad (44)$$

Three vibrational states are the initial vibrational state $|i\rangle$, intermediate vibrational state $|v\rangle$ and the final vibrational state $|f\rangle$.

$$H_{\text{mol}}^{\text{v}}|i\rangle = E_i^0|i\rangle \quad (45)$$

$$H_{\text{mol}}^{\text{v}}|v\rangle = E_v^0|v\rangle \quad (46)$$

$$H_{\text{mol}}^{\text{v}}|f\rangle = E_f^0|f\rangle \quad (47)$$

With the first-order perturbation theory, we obtain an expression for the first-order intermediate electronic state (Herzberg-Teller expansion)

$$|e\rangle = \sum_{s \neq g} [s_0 \left| \left(\frac{\partial H_{\text{mol}}^{ev}}{\partial Q_k} \right)_0 Q_k \right| e_0] |s_0\rangle$$

Introducing all into the KHD formula, we obtain an expression for a Raman scattering tensor under a resonance condition (Albrecht 1961).

$$\alpha_{\rho\sigma} = A + B$$

$$A = \sum_{e \neq g} \sum_{\nu} \frac{[g_0 | D_\sigma | e_0][e_0 | D_\rho | g_0]}{E_e^0 + E_\nu^0 - E_g^0 - E_i^0 - E_i - i\Gamma_e} (i | \nu)(\nu | f)$$

$$B = \sum_{e \neq g} \sum_{\nu} \sum_{\lambda} \frac{[g_0 | D_\sigma | s_0][s_0 | (\partial H_{ev} / \partial Q_\lambda)_0 | e_0][e_0 | D_\rho | g_0]}{E_e^0 + E_\nu^0 - E_g^0 - E_i^0 - E_i - i\Gamma_e} (i | Q_\lambda | \nu)(\nu | f)$$

$$+ \sum_{e \neq g} \sum_{\nu} \sum_{\lambda} \frac{[g_0 | D_\sigma | e_0][e_0 | (\partial H_{ev} / \partial Q_\lambda)_0 | s_0][s_0 | D_\rho | g_0]}{E_e^0 + E_\nu^0 - E_g^0 - E_i^0 - E_i - i\Gamma_e} (i | \nu)(\nu | Q_\lambda | f)$$

Theory of Raman Scattering (3)

Albrecht's vibronic theory of resonance Raman Scattering

A. C. Albrecht, J. Chem. Phys. 34, 1476 (1961).

$$a_{\rho\sigma} \sim A + B$$

A term: Franck-Condon term

Totally symmetric modes

high overtones

B term: Vibronic coupling

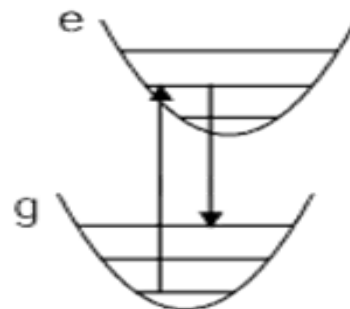
Non-totally symmetric modes

overtones?

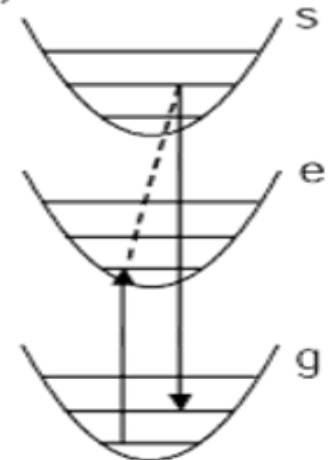
A. C. Albrecht
(1927-2002)



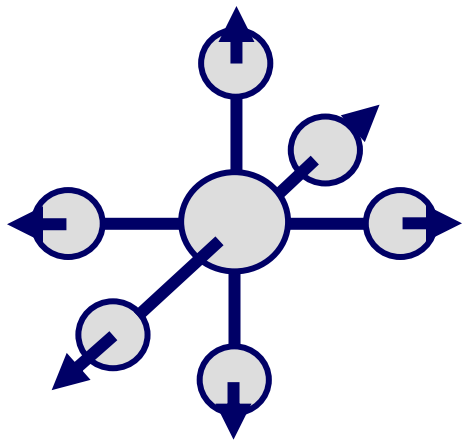
(a)



(b)



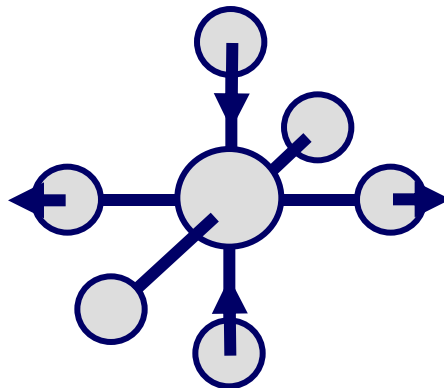
Raman Active Vibrations of MX_6 Octahedral Complexes



ν_1
(\mathbf{a}_{1g})

$$\mathbf{a}_{1g} \sim \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

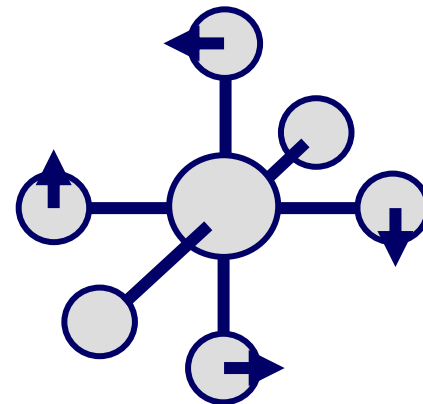
$$\rho=0$$



ν_2
(\mathbf{e}_g)

$$\mathbf{e}_g \sim \begin{pmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

$$\rho=0.75$$



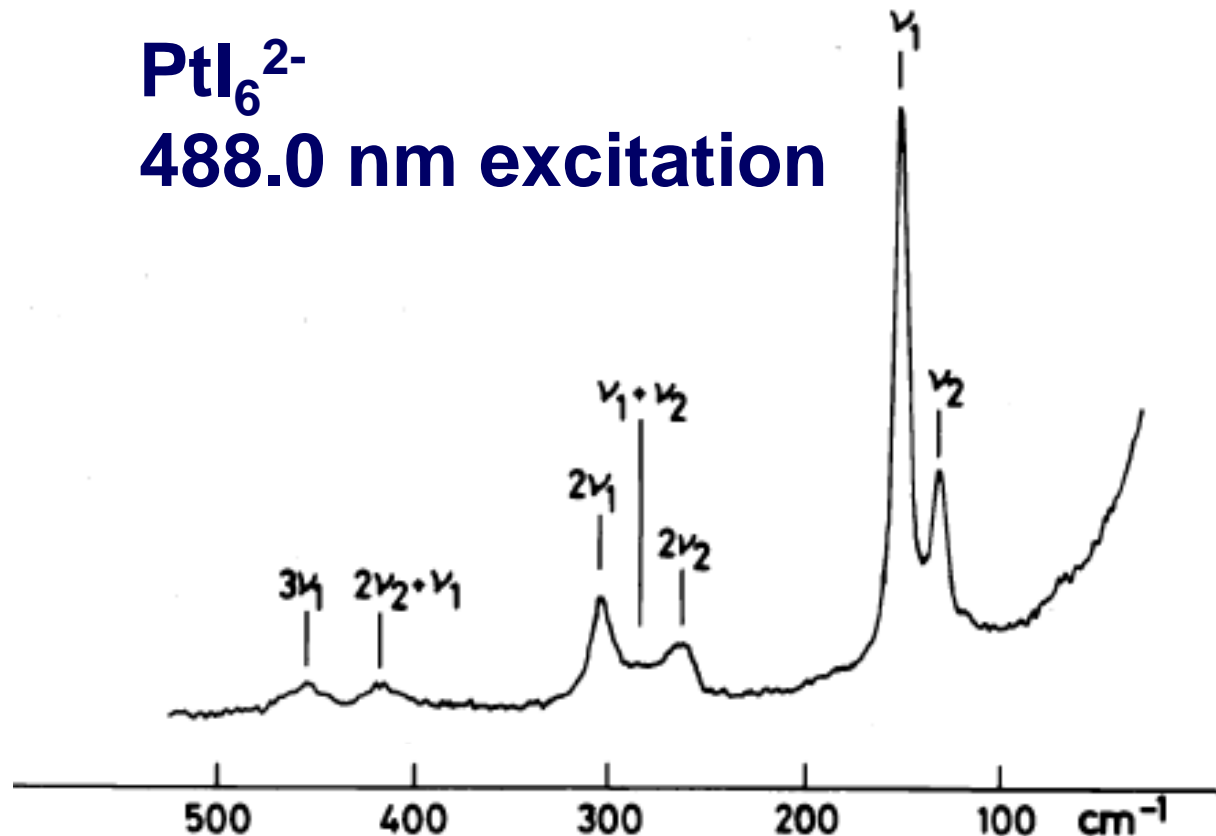
ν_5
(\mathbf{t}_{2g})

$$\mathbf{t}_{2g} \sim \begin{pmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

$$\rho=0.75$$

Resonance Raman spectrum of PtI_6^{2-}

PtI_6^{2-}
488.0 nm excitation

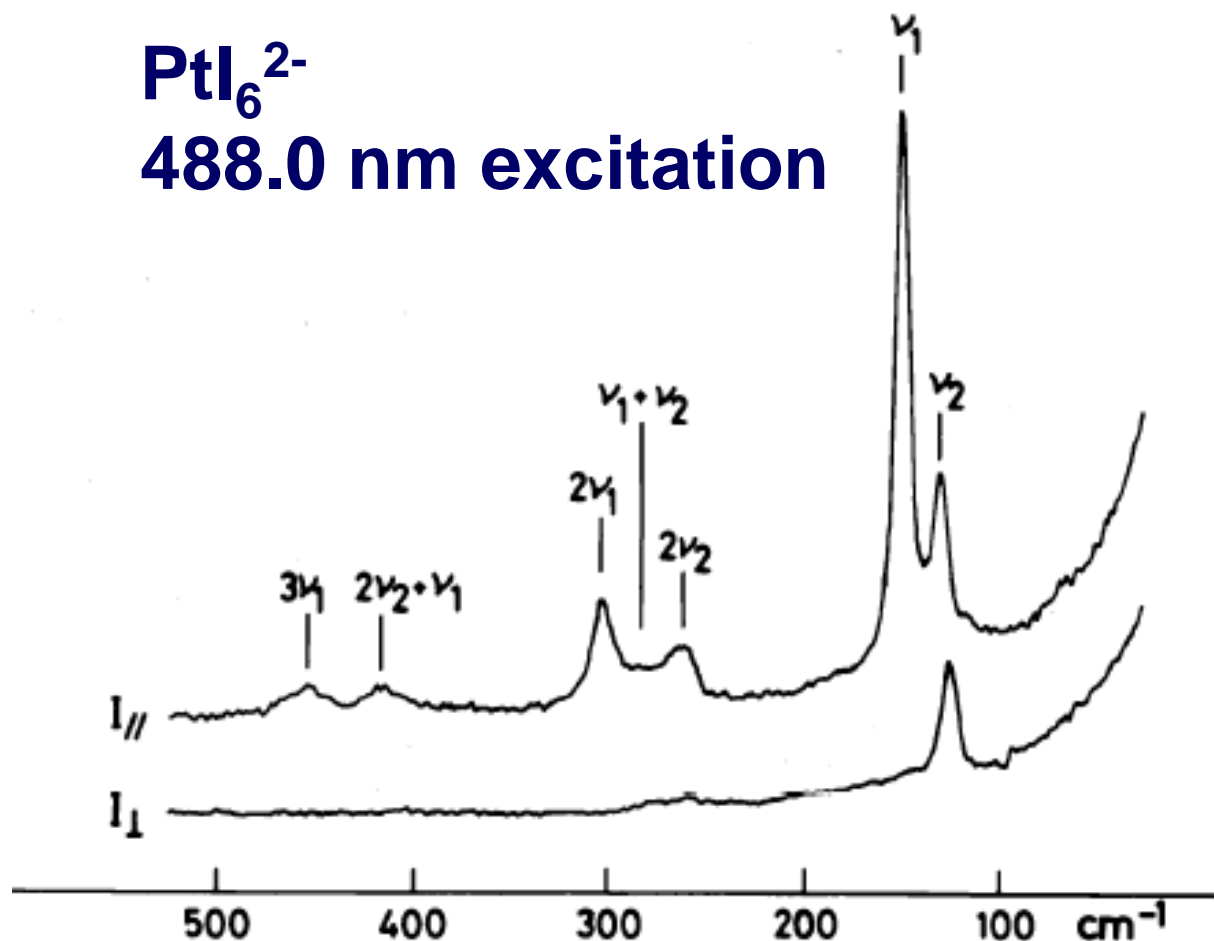


Totally symmetric mode ($\nu_1, 2\nu_1, 3\nu_1$) → **A term**

Non-totally symmetric mode ($\nu_2, 2\nu_2, \nu_1 + \nu_2, 2\nu_1 + \nu_2$) → **B term**

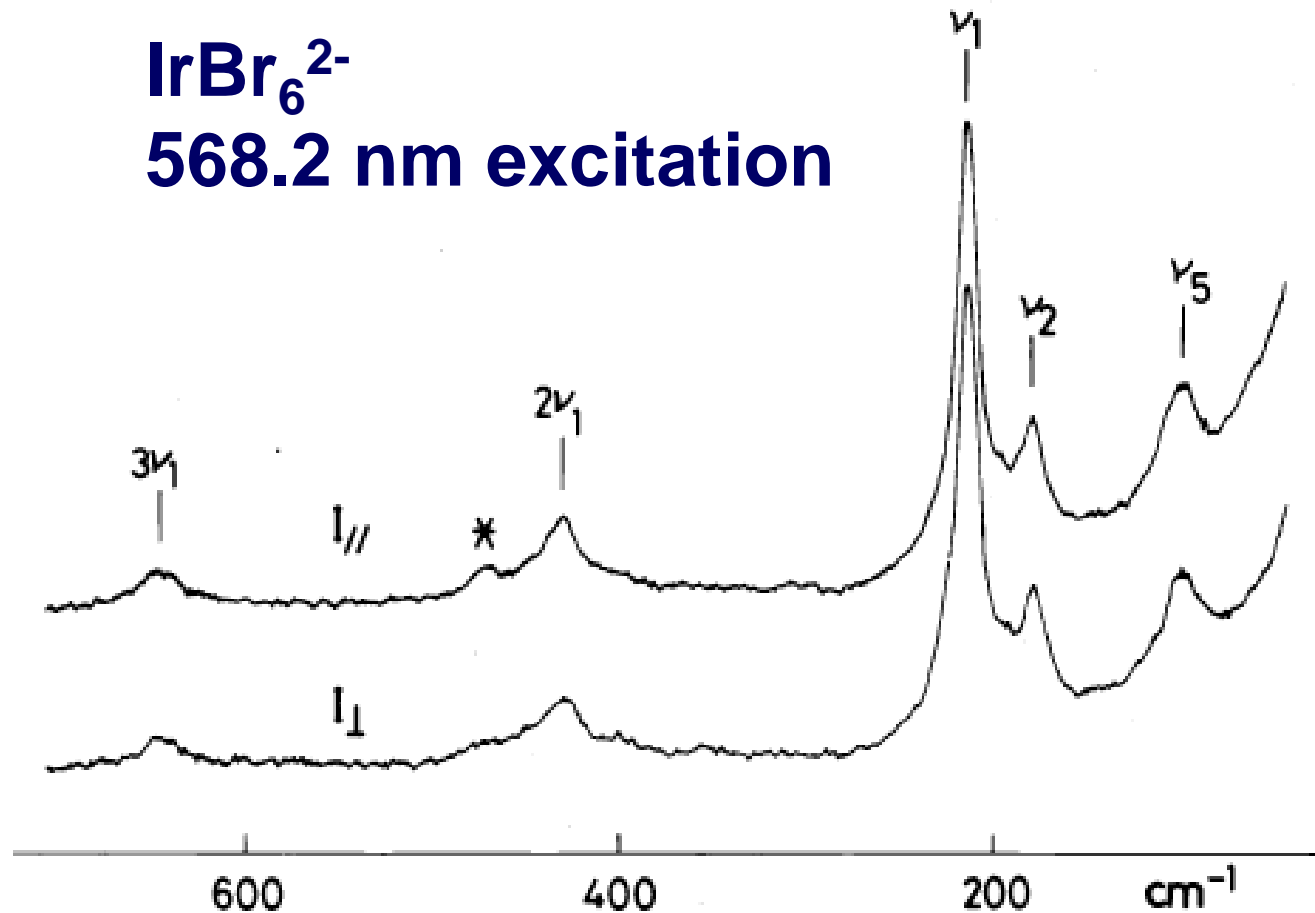
Polarized Resonance Raman Spectra of PtI_6^{2-}

**PtI_6^{2-}
488.0 nm excitation**



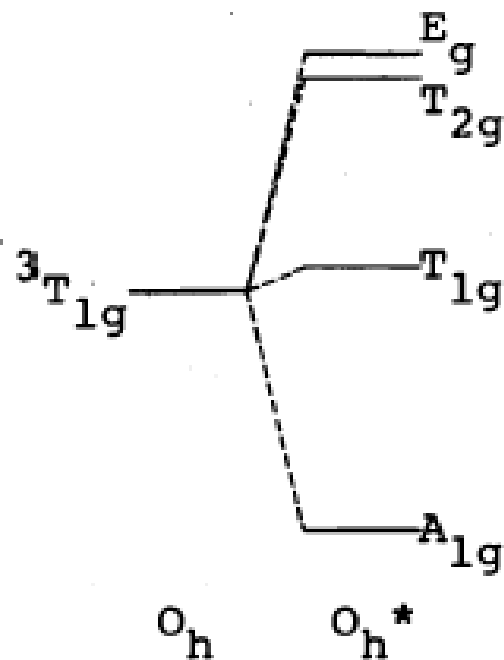
v_1 , $2v_1$, $3v_1$ bands $\rho=0$; v_2 band $\rho=0.75$

Polarized Resonance Raman Spectra of IrBr_6^{2-}

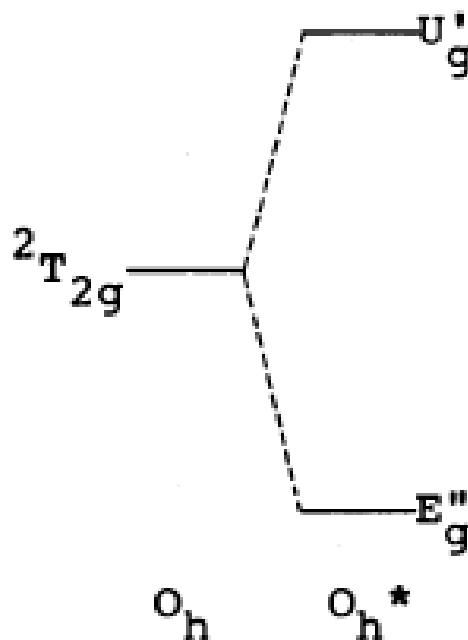


$\rho=1$ for all bands; forgot to rotate the analyzer?

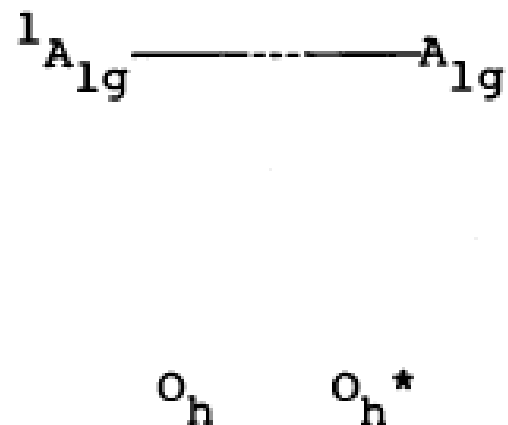
Ground-state Electron Configuration and Electronic States of Octahedral MX_6 Complexes



d^4 complexes



d^5 complexes

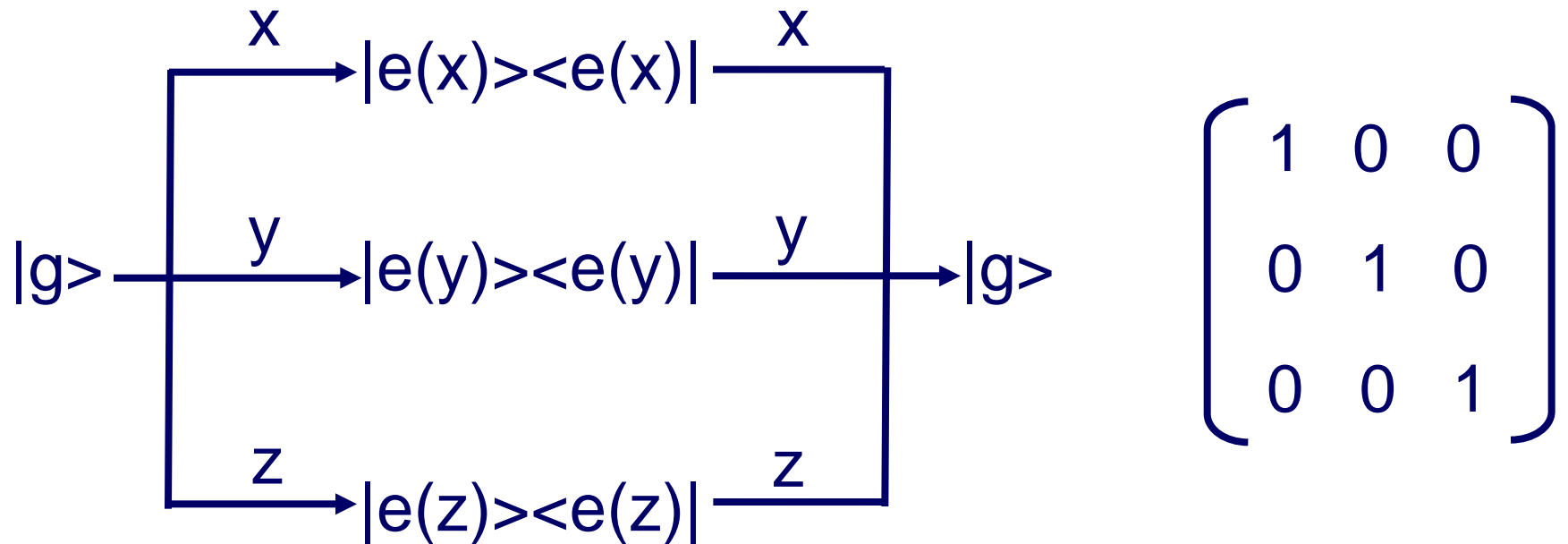


d^6 complexes



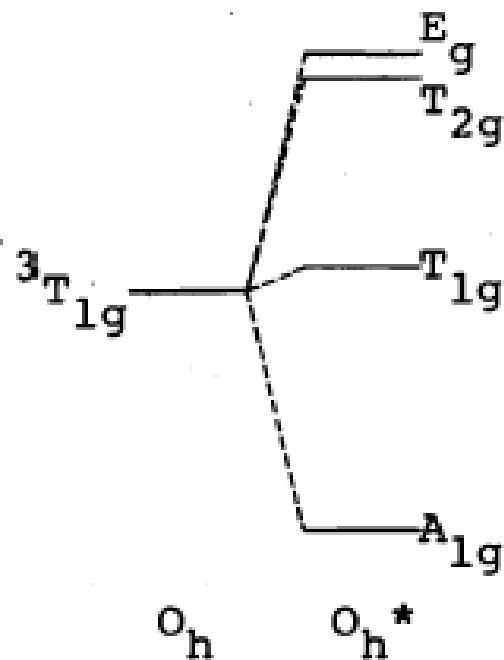
Raman Scattering Tensor and Depolarization Ratio of the Totally Symmetric Mode of Non-degenerate PtI_6^{2-} Ion

$$\Gamma_g = a_{1g}, \quad \Gamma_e = t_{1u}$$

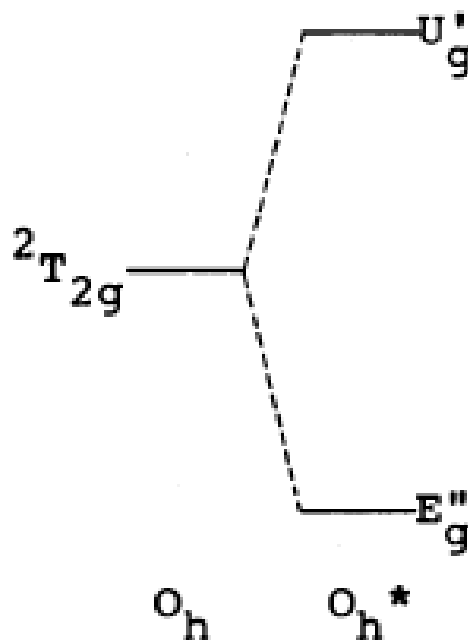


$$G_0=3, \quad G_a=0, \quad G_s=0 \quad \rho=3G_s/(10G_0+4G_s)=0$$

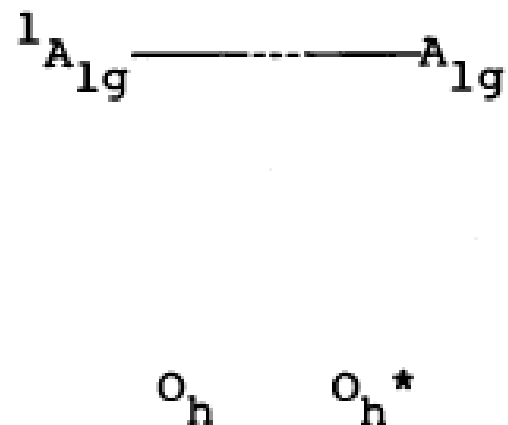
Ground-state Electron Configuration and Electronic States of Octahedral MX_6 Complexes



d^4 complexes



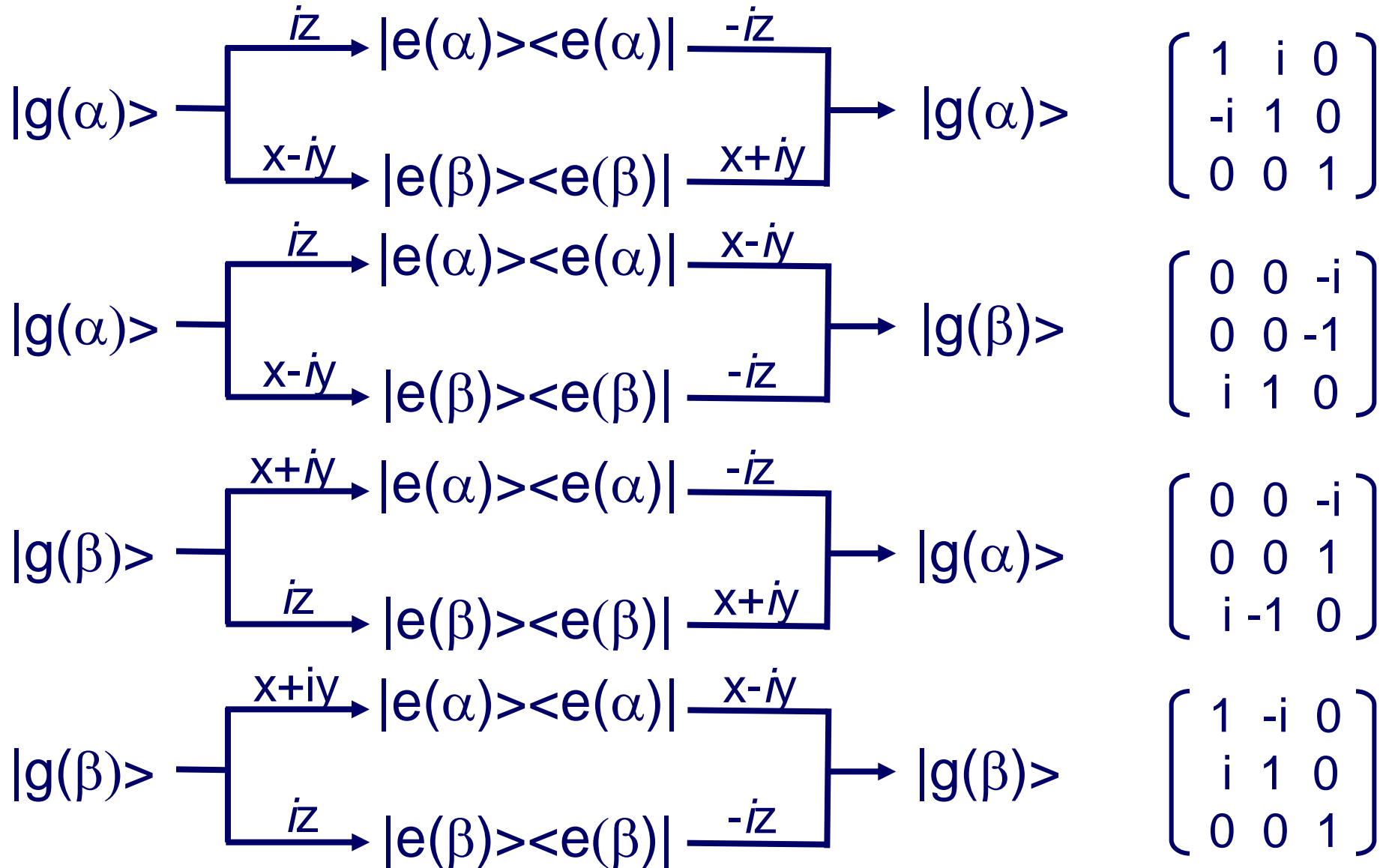
d^5 complexes



d^6 complexes



Raman Tensors for the a_{1g} Vibrational Transitions of MX_6 in an E_g Ground Electronic State



Raman Tensors for the a_{1g} Vibrational Transitions of MX_6 in an E_g Ground Electronic State and Depolarization Ratio

$$\begin{array}{l}
 |g(\alpha)\rangle \longrightarrow |g(\alpha)\rangle \quad \begin{pmatrix} 1 & i & 0 \\ -i & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix} \quad G_0=3, G_a=2, G_s=0 \\
 |g(\alpha)\rangle \longrightarrow |g(\beta)\rangle \quad \begin{pmatrix} 0 & 0 & -i \\ 0 & 0 & -1 \\ i & 1 & 0 \end{pmatrix} \quad G_0=0, G_a=4, G_s=0 \\
 |g(\beta)\rangle \longrightarrow |g(\alpha)\rangle \quad \begin{pmatrix} 0 & 0 & -i \\ 0 & 0 & 1 \\ i & -1 & 0 \end{pmatrix} \quad G_0=0, G_a=4, G_s=0 \\
 |g(\beta)\rangle \longrightarrow |g(\beta)\rangle \quad \begin{pmatrix} 1 & -i & 0 \\ i & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix} \quad G_0=3, G_a=2, G_s=0
 \end{array}$$

$$G_0=6, G_a=12, G_s=0$$

$$\rho=(3G_s+5G_a)/(10G_0+4G_s)=1$$

Symmetry of Raman Scattering Tensor

Irreducible representations:

Γ_i : the initial states, Γ_f : the final state, Γ_R : Raman tensor

$$\Gamma_R = \Gamma_i \times \Gamma_f$$

Vibrational Raman Scattering:

$\Gamma_i = \gamma_g \times \gamma_1$, $\Gamma_f = \gamma_g \times \gamma_v$ and therefore $\Gamma_R = \gamma_g \times \gamma_g \times \gamma_v$

where γ_g : the ground electronic state and γ_v : vibrational state

A_{1g} Vibrational Raman Scattering:

$d_6 \text{PtI}_6^{2-}$ $\gamma_g = a_{1g}$, $\gamma_v = a_{1g}$ and therefore $\Gamma_R = a_{1g}$ $\rho = 0$

$d_5 \text{IrBr}_6^{2-}$ $\gamma_g = e_g$, $\gamma_v = a_{1g}$ and therefore $\Gamma_R = a_{1g} + t_{1g}$ $0 < r < \infty$

Depolarization Ratio in Vibrational Raman Scattering

Polarizability theory (Placzek, 1934)

1) Non-resonant condition, 2) Non-degenerate condition

Totally symmetric modes: $G_0 \neq 0, G_a = 0, G_s \neq 0 \implies 0 \leq \rho < 0.75$

Non-totally symmetric modes: $G_0 = 0, G_a = 0, G_s \neq 0 \implies \rho = 0.75$

Breakdown of the Placzek polarizability theory

1) Non-resonant condition (Spiro, 1972)

Non-totally symmetric modes : $G_0 = 0, G_a \neq 0, G_s \neq 0 \quad 0.75 < \rho < \infty$

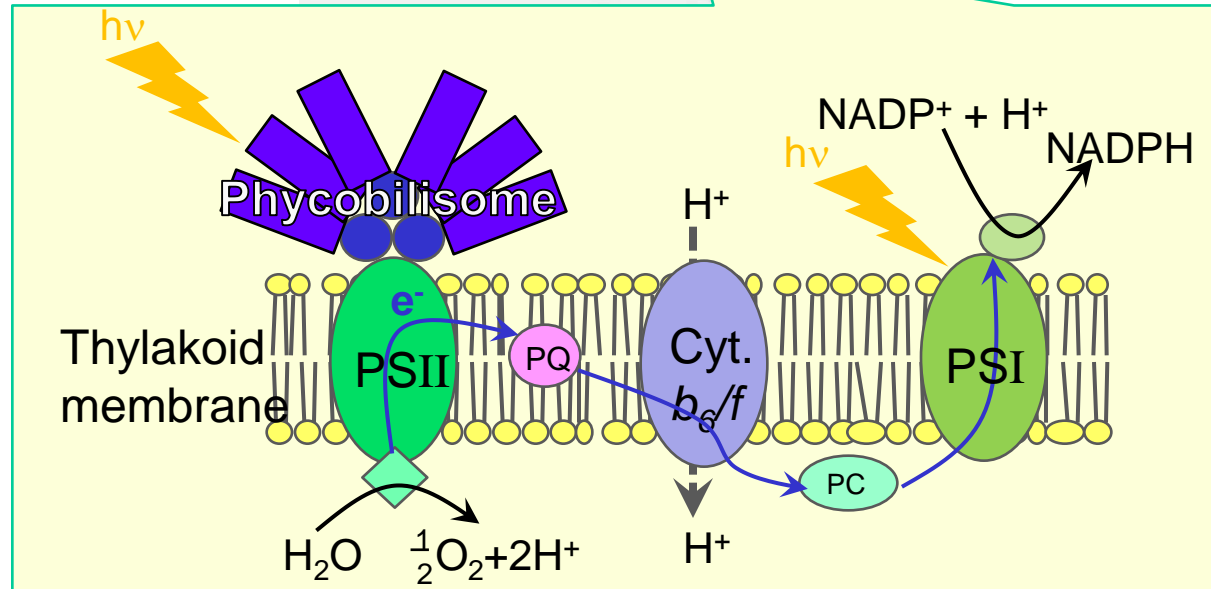
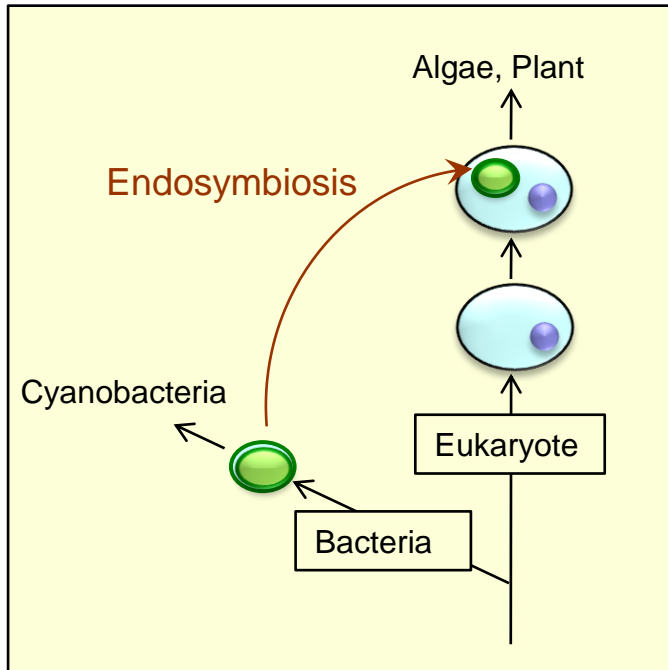
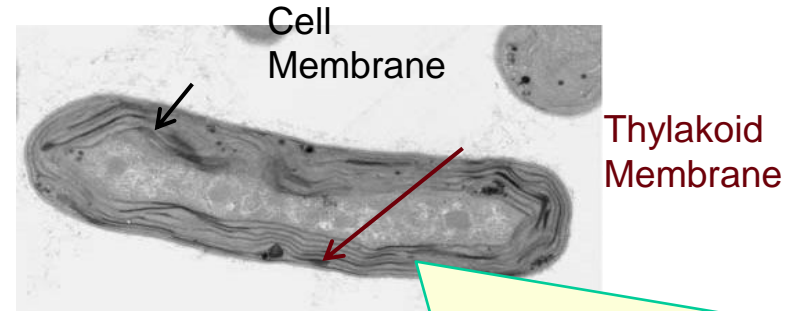
2) Non-degenerate condition (Hamaguchi, Harada, Shimanouchi, 1975)

Totally symmetric modes : $G_0 \neq 0, G_a \neq 0, G_s = 0 \quad 0 < \rho < \infty$

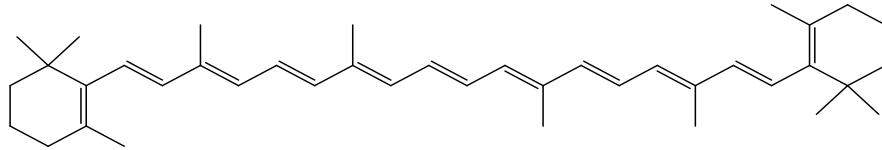
Placzek's prediction was proved after 40 years to establish firmly the theoretical basis of Raman spectroscopy.

Cyanobacteria

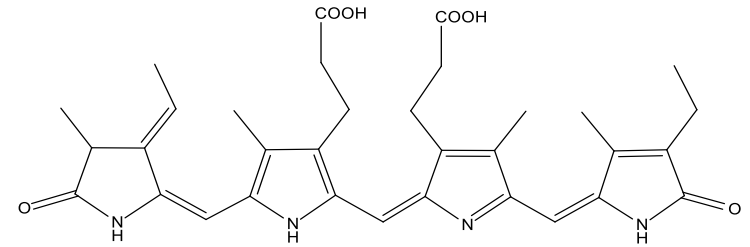
- Photosynthetic microorganism
- Origin of chloroplast
- Model organism for photosynthesis research



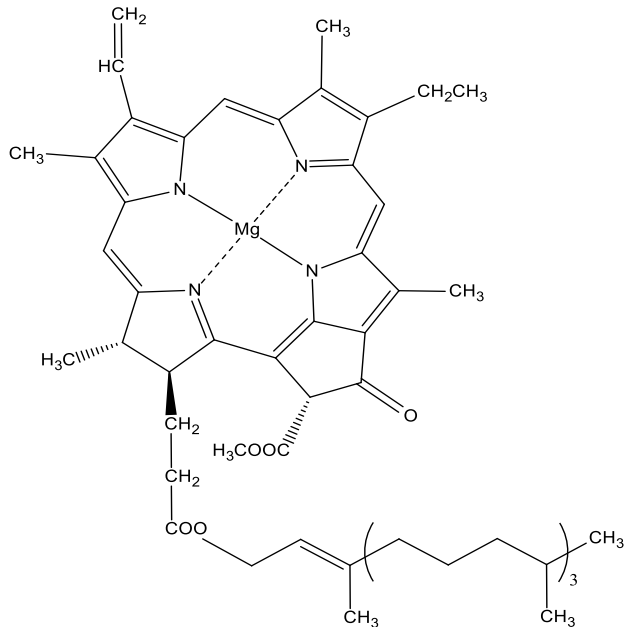
Pigments contained in cyanobacteria



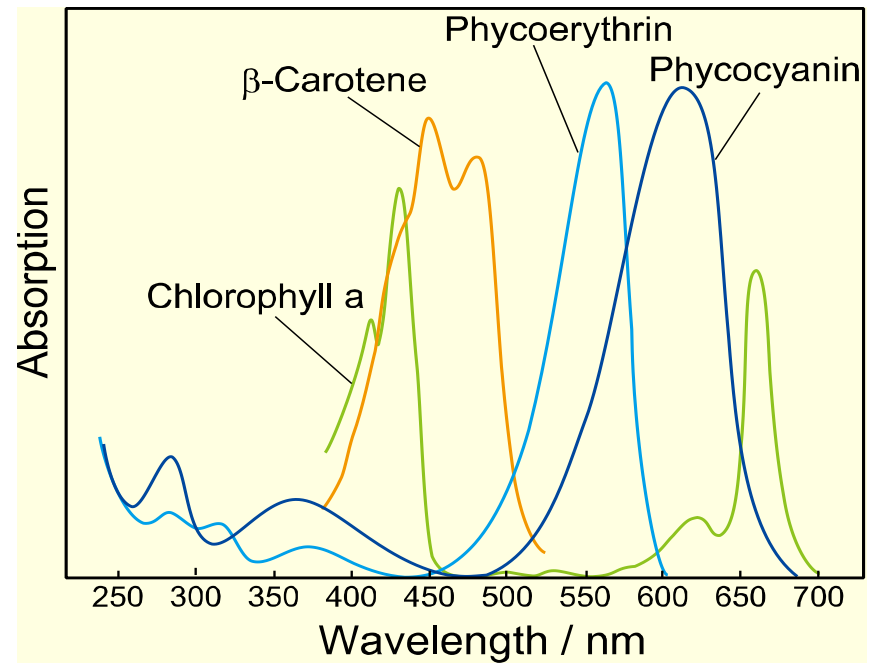
Carotenoid



Phycobilin



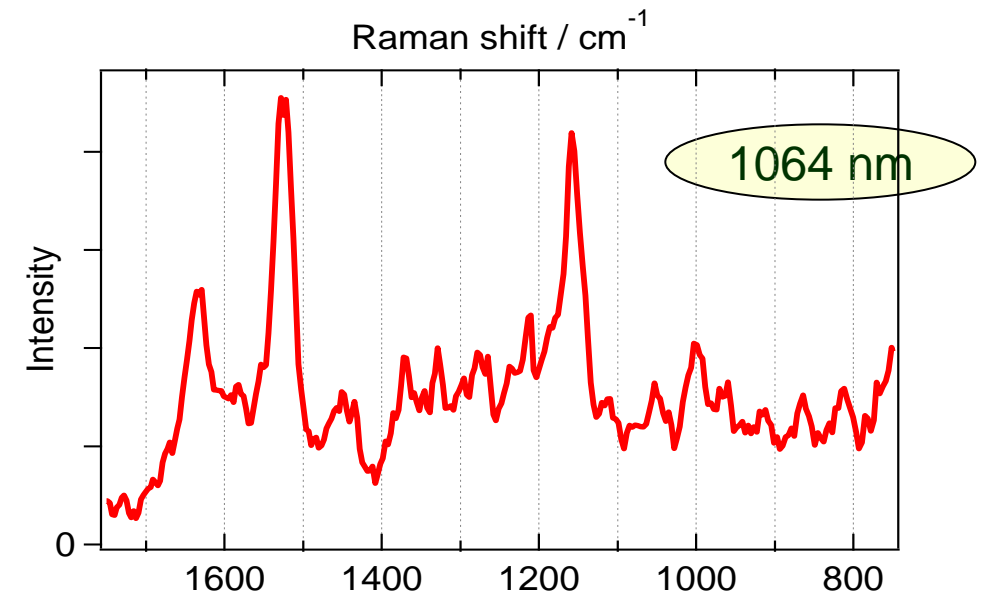
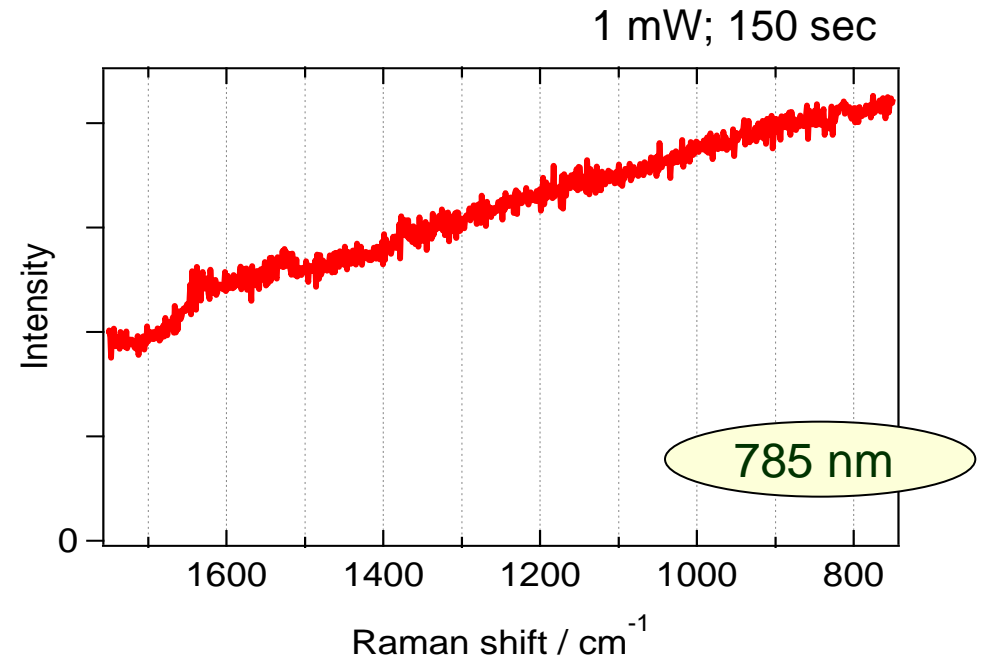
Chlorophyll a



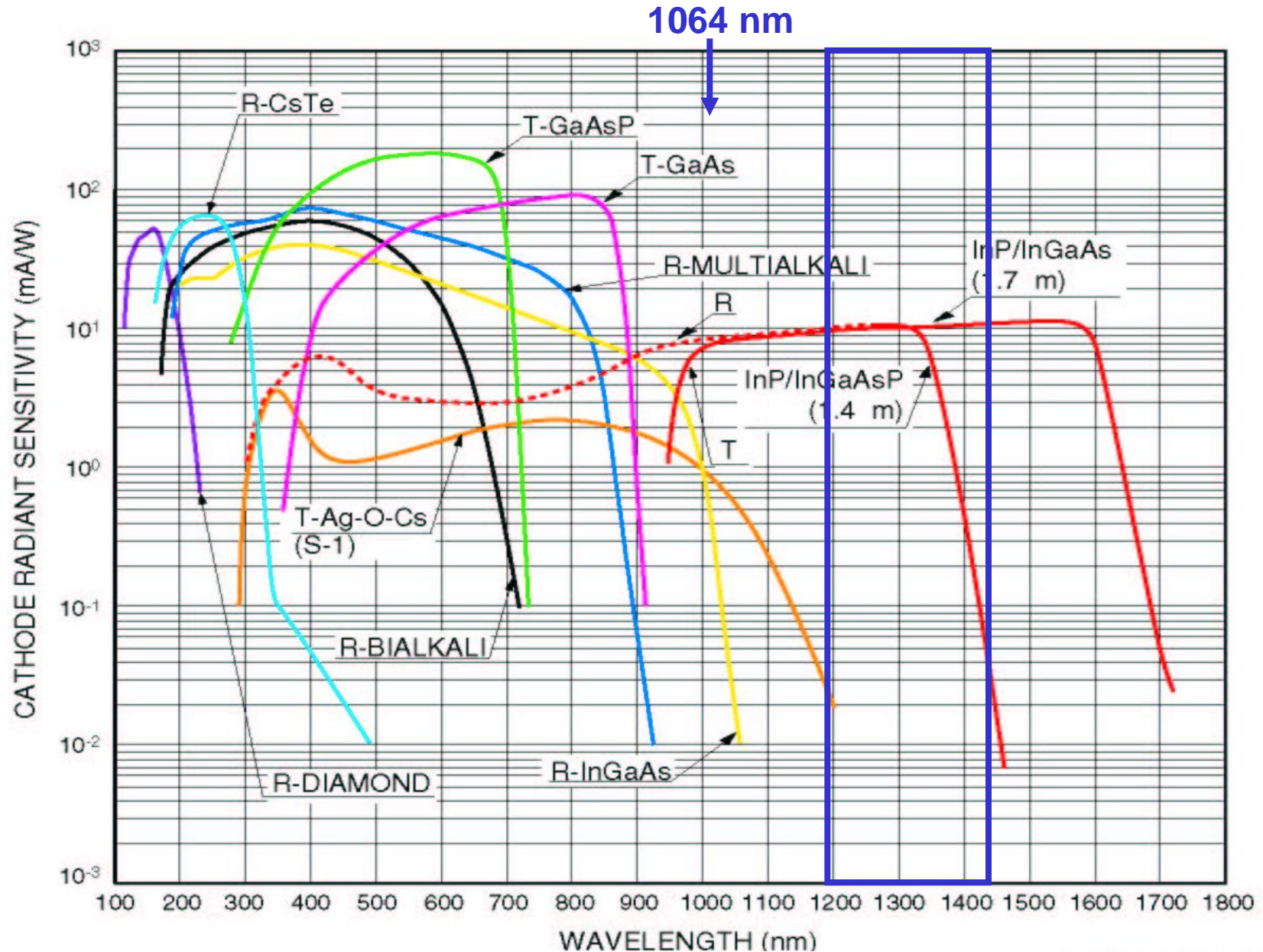
NIR Raman measurements of cyanobacteria

Thermosynechococcus elongatus

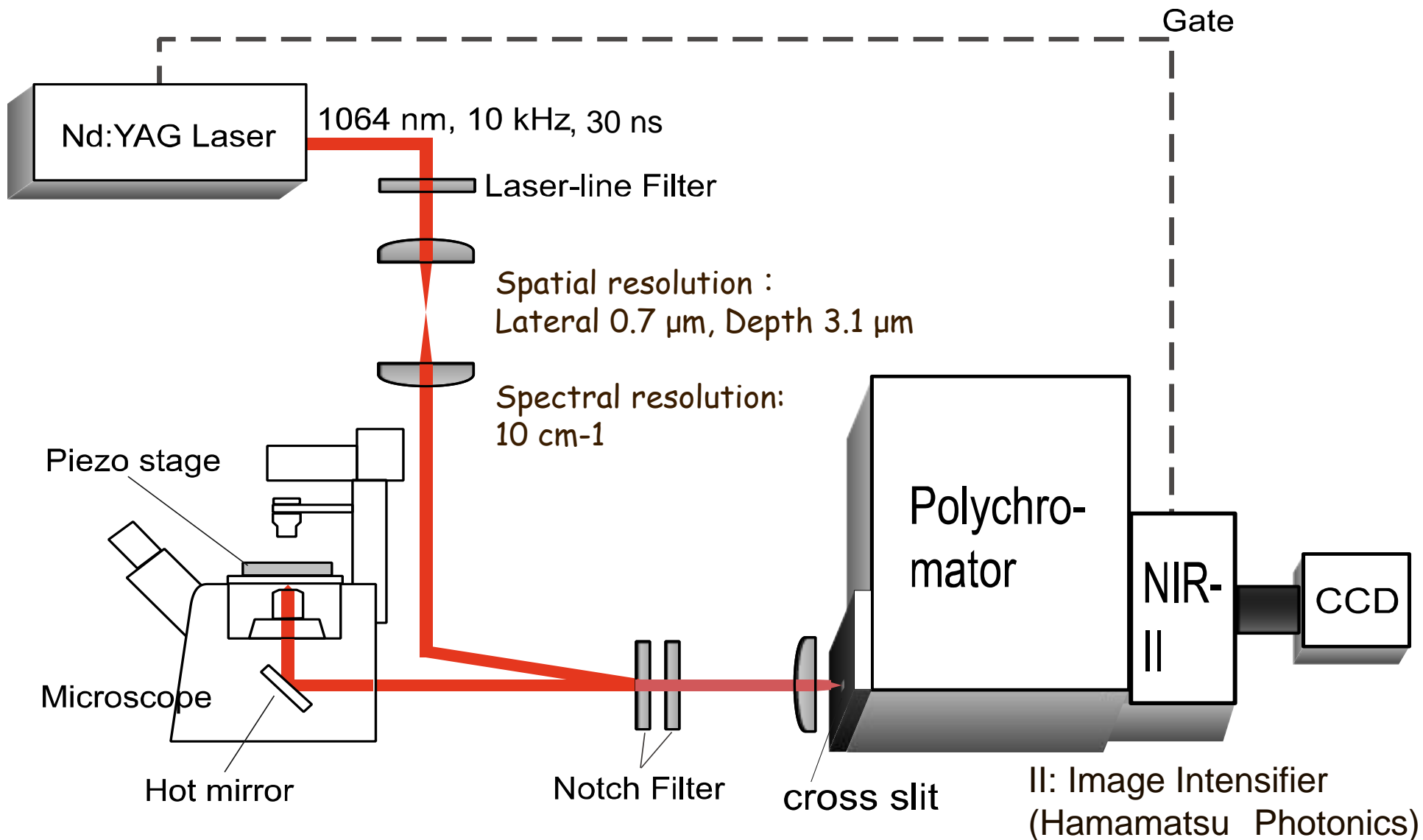
- Thermophilic cyanobacteria
(Unicellular rod-shaped)
- Well-established model organism
 - Entire genome sequenced



1064 nm Excited Raman Spectroscopy with InP/InGaAsP Multichannel Detector

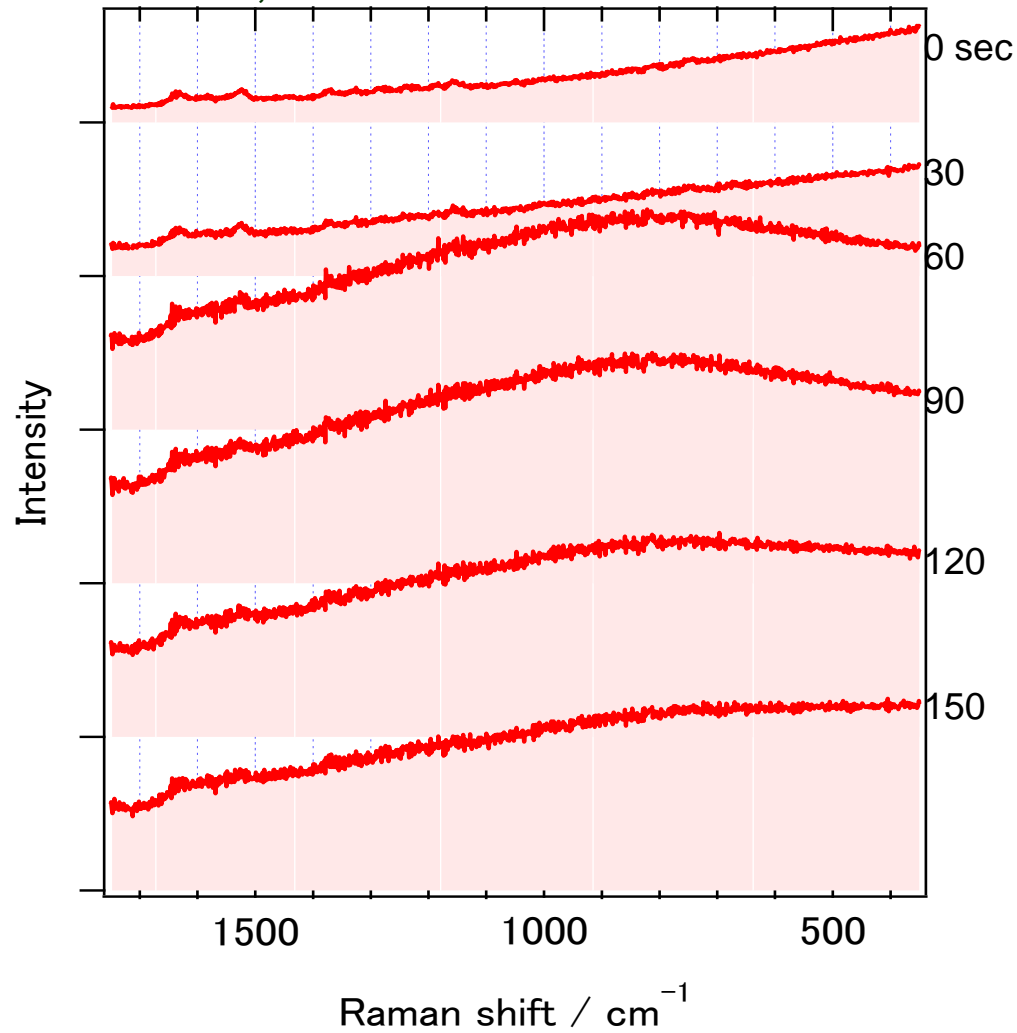


1064 nm Excited Multichannel Raman Microspectrometer

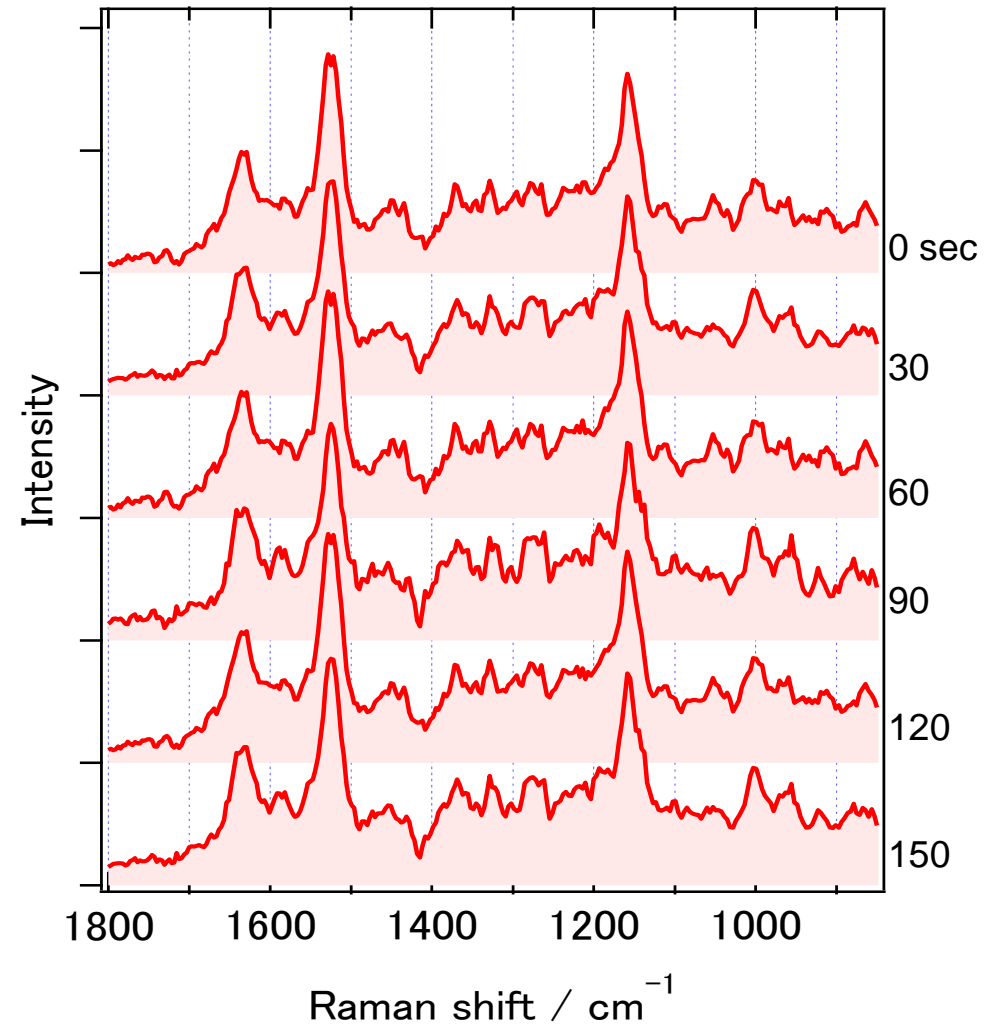


NIR Raman measurements of cyanobacteria

785 nm; 0.6 mW



1064 nm; 0.6 mW



Deep near-infrared excitation is needed for avoiding the photodamage.

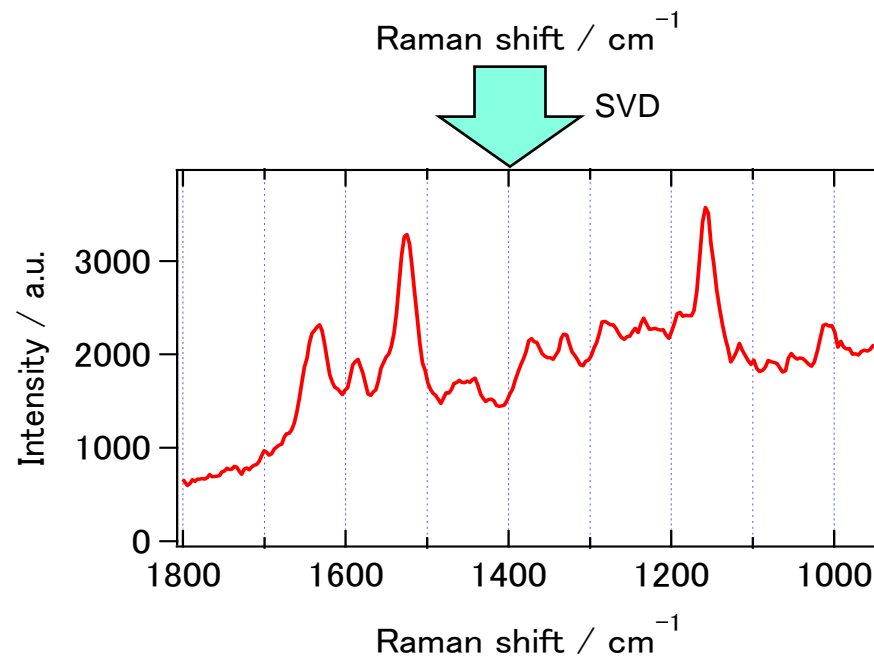
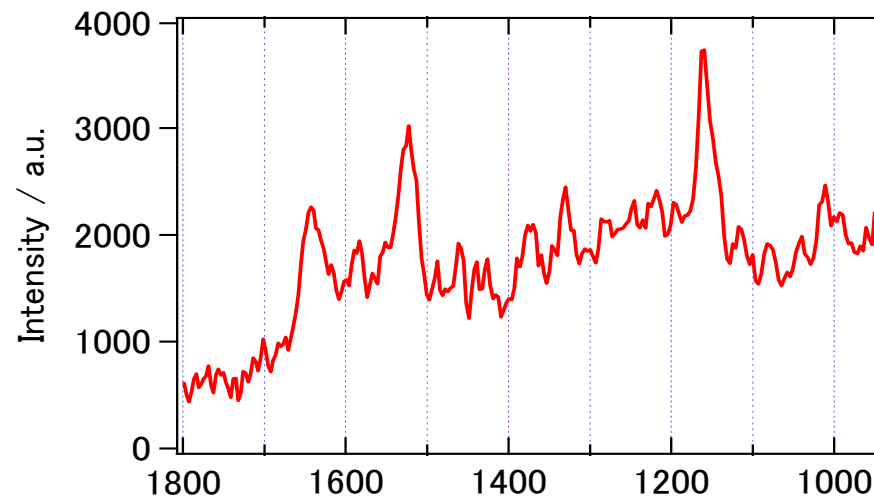
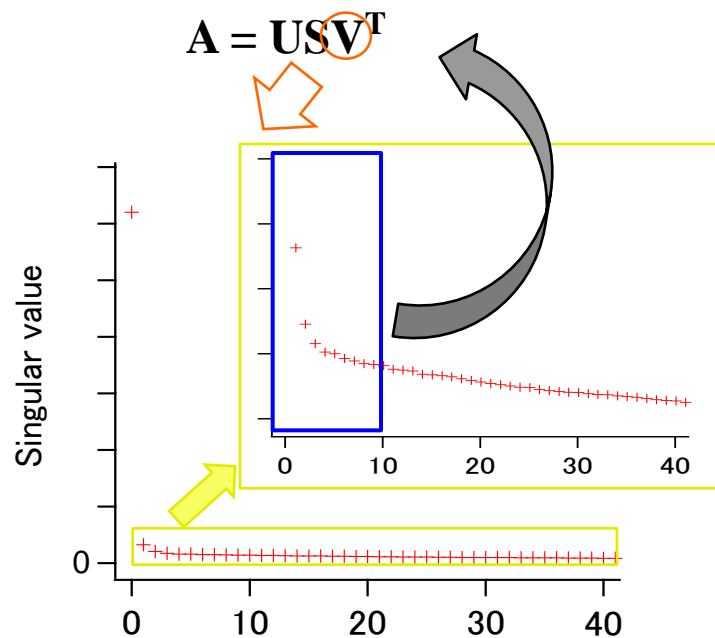
Space-resolved Measurements and SVD Noise Filtering



13 x 22 pix
(0.3 μ m interval)

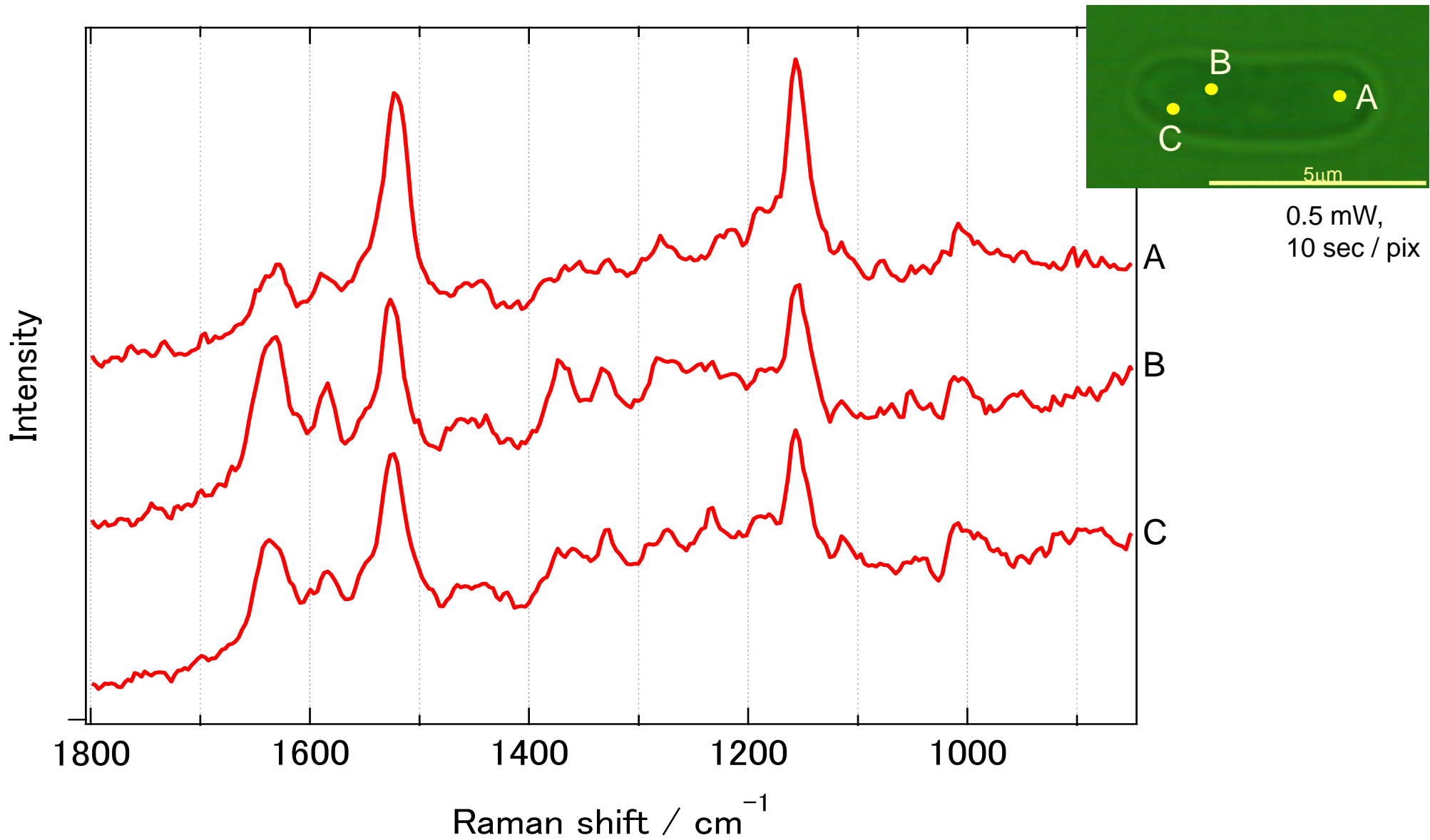
0.5 mW,
10 sec / pix

○ Singular value decomposition as noise filter¹⁾

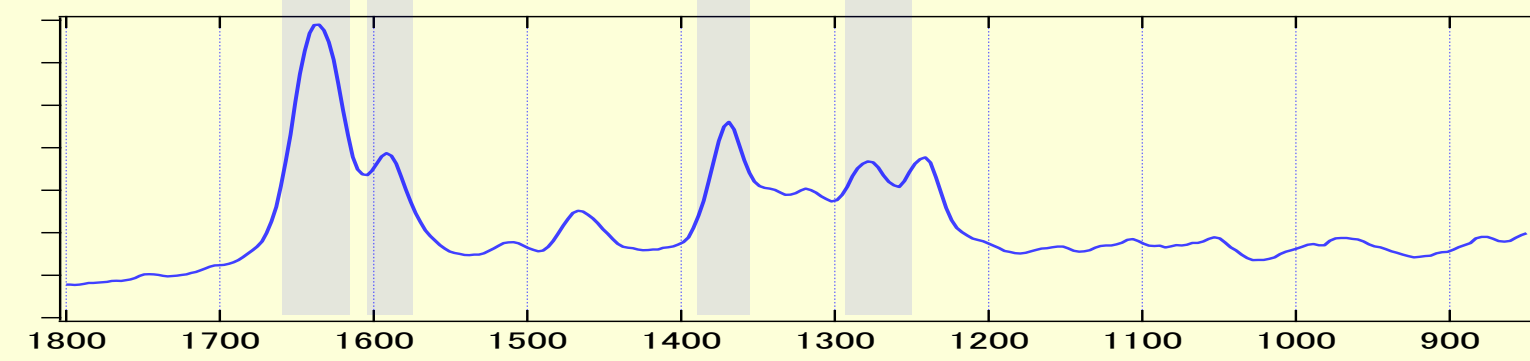
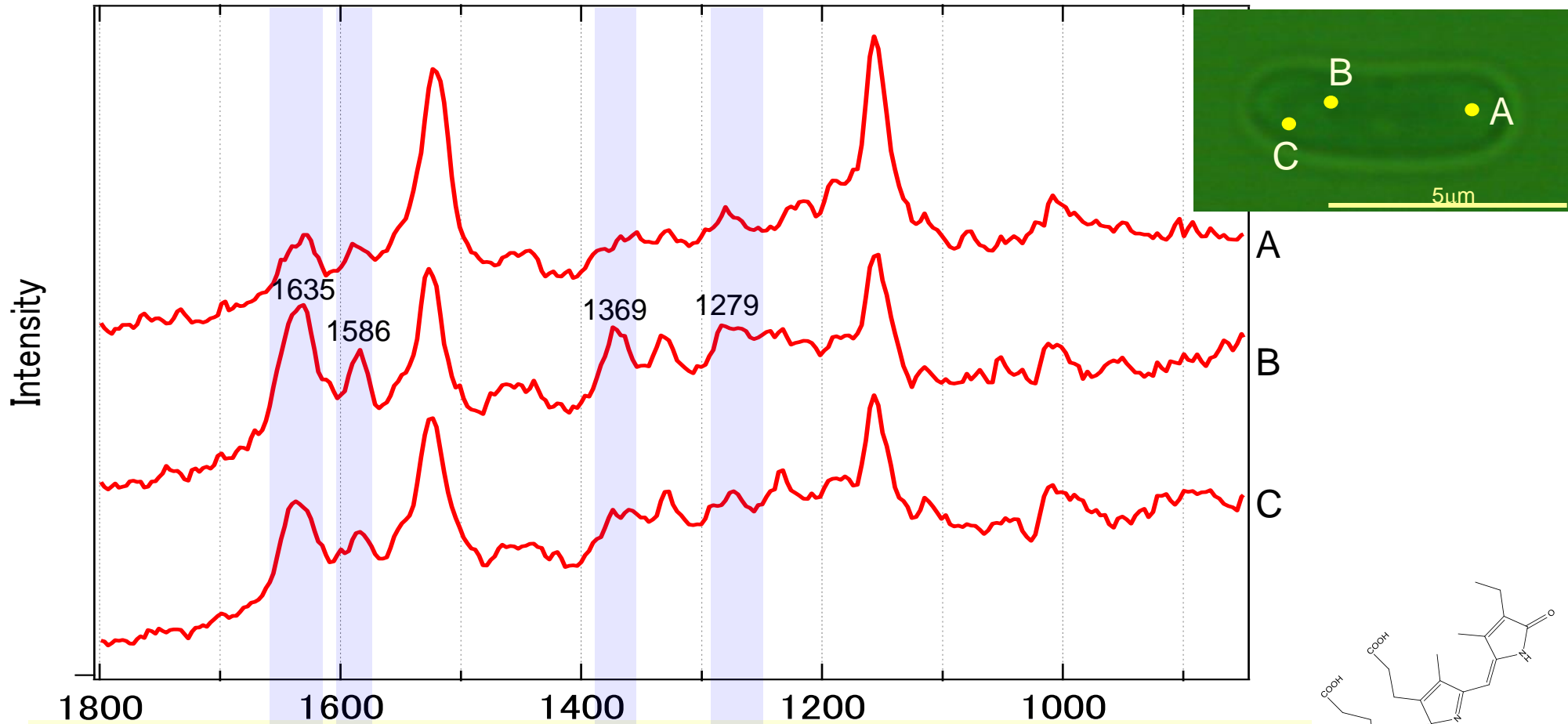


1) N. Uzunbajakava, C. Otto, et al. *Biophysical Journal* (2003) 3968-3981.

Space-resolved Raman Spectra within a Cell

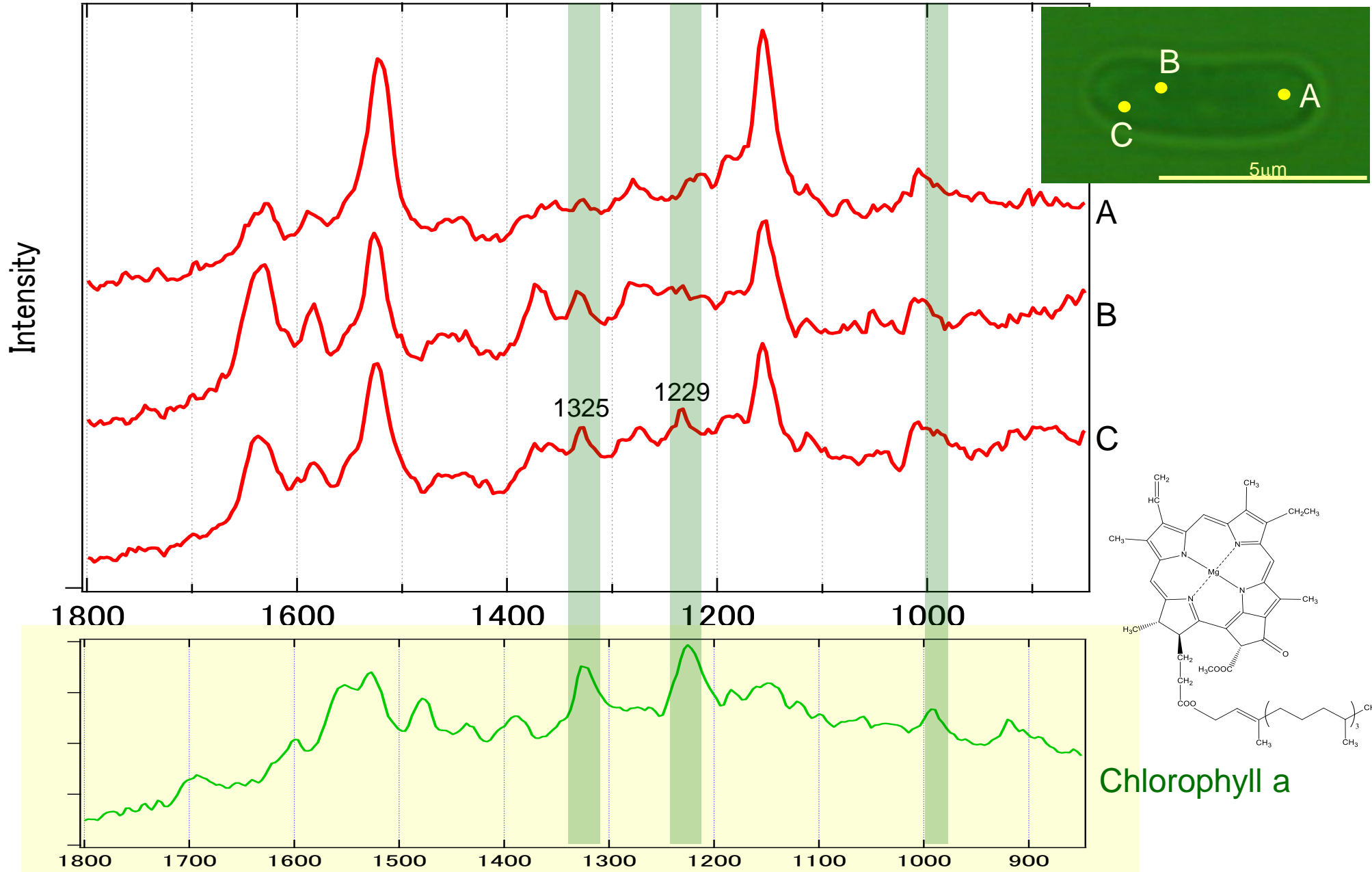


Band assignments

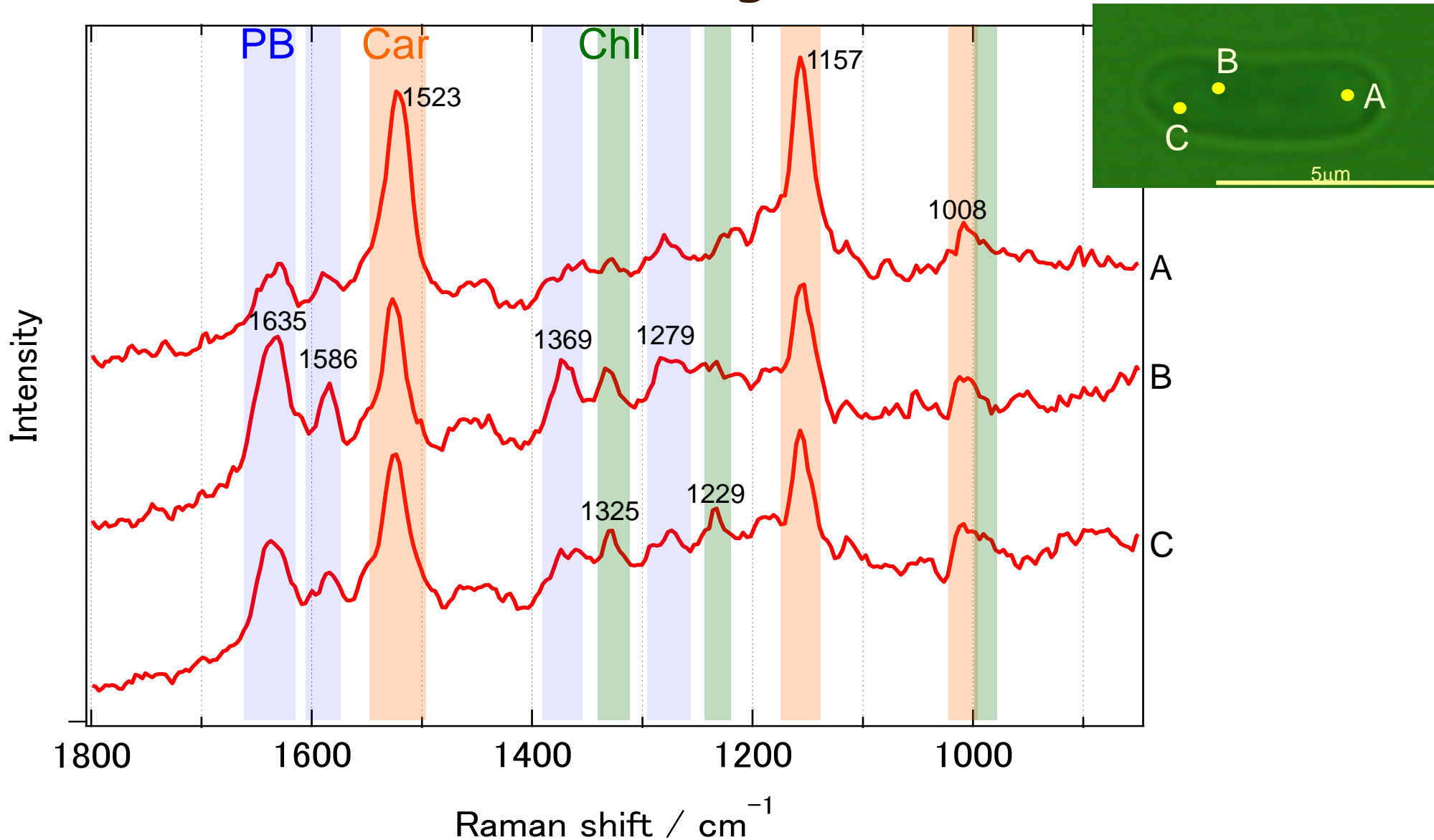


Phycobilin

Band assignments



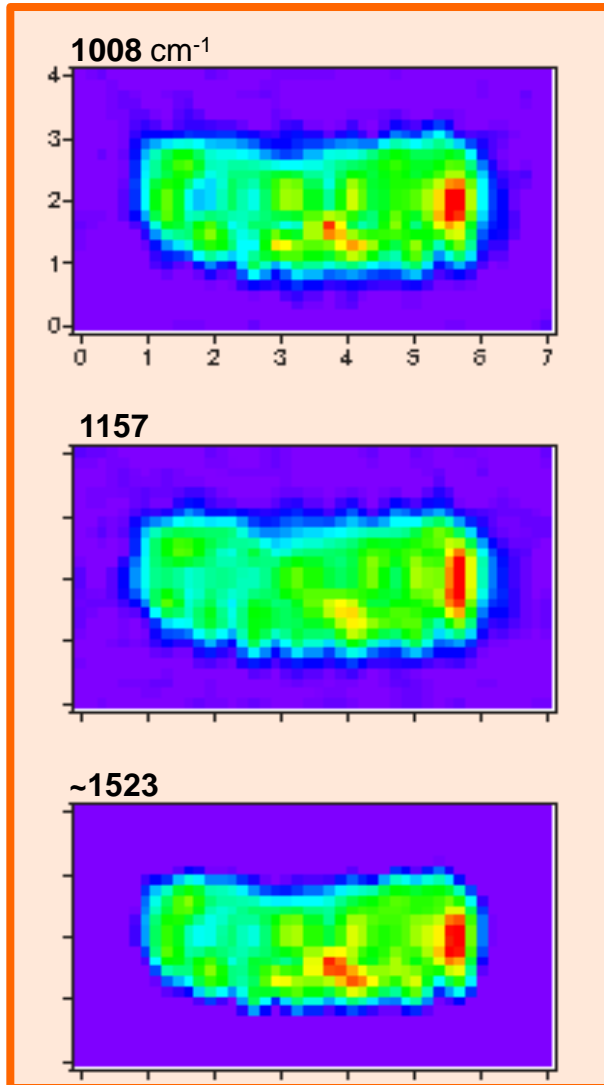
Band assignments



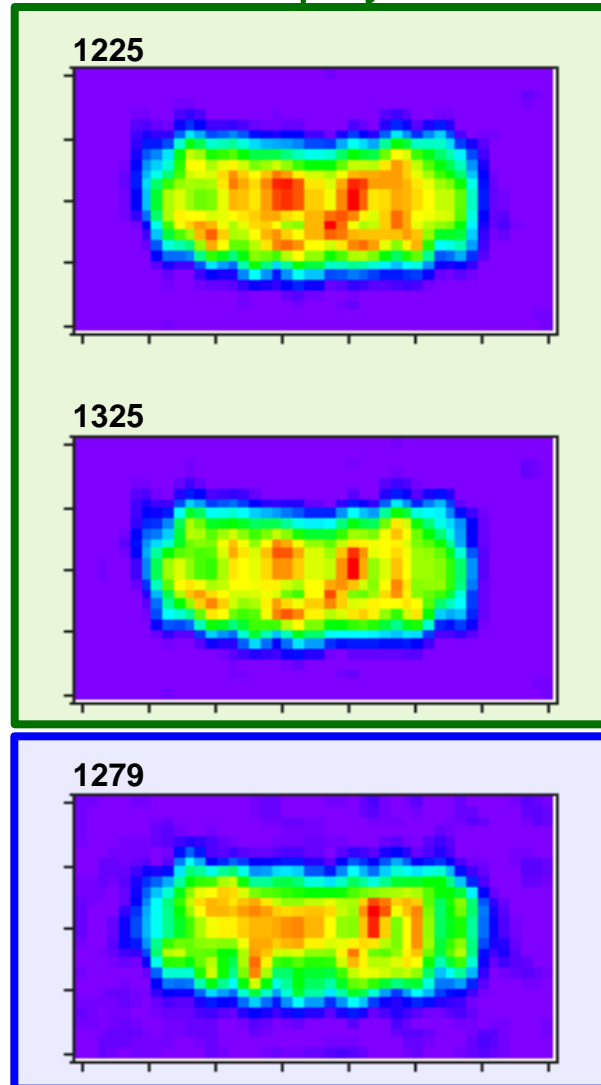
Almost all bands are assignable to the three photosynthetic pigments
← Due to pre-resonance effect.

Raman mapping images

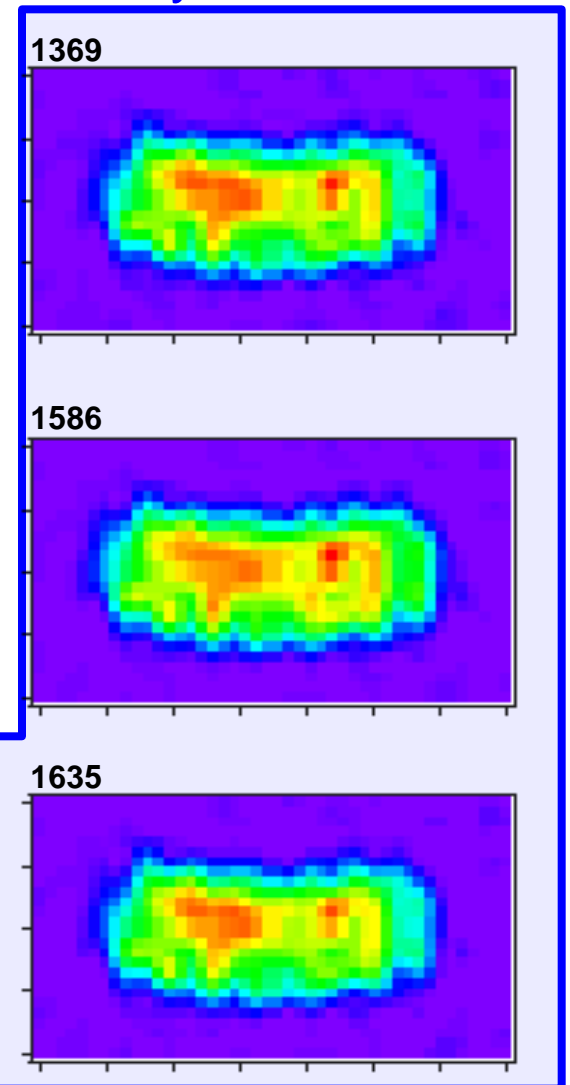
Carotenoid



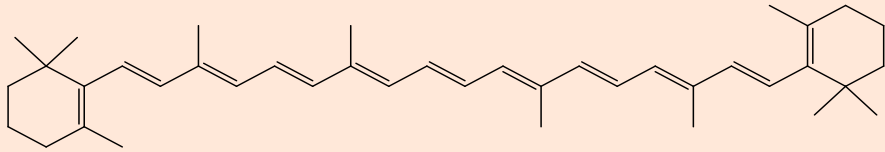
Chlorophyll



Phycobilin

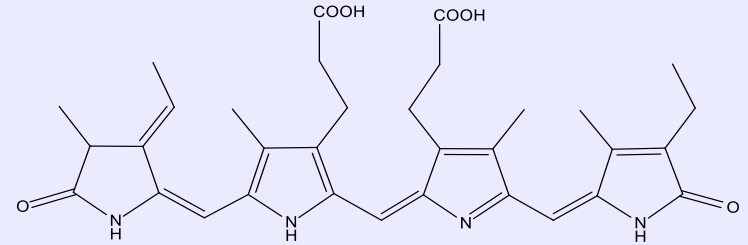


Functions of photosynthetic pigments



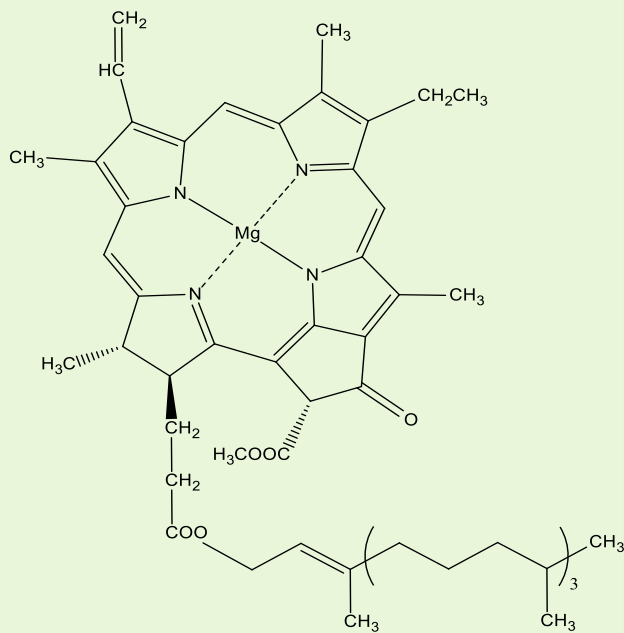
Carotenoid

Light harvesting
Antioxidant
Photoprotection



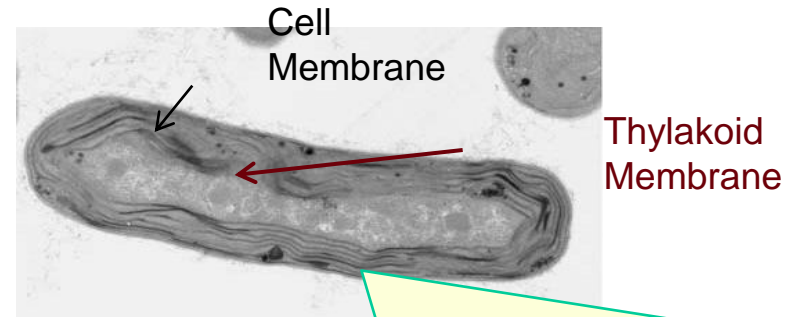
Phycobilin

Light harvesting



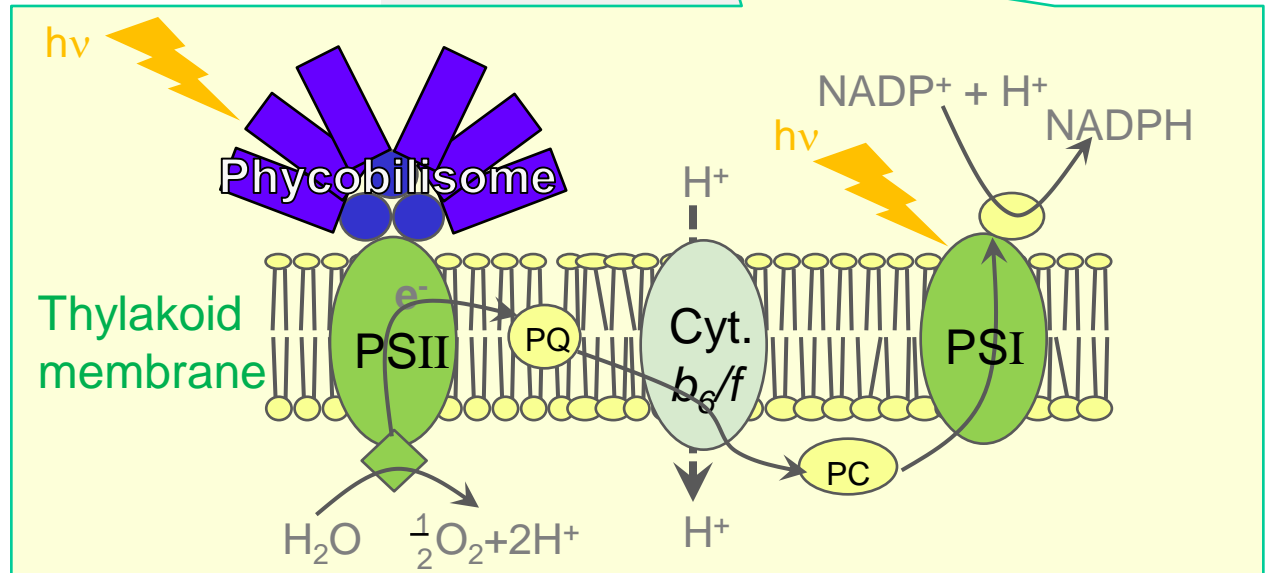
Chlorophyll a

Reaction center
Light harvesting



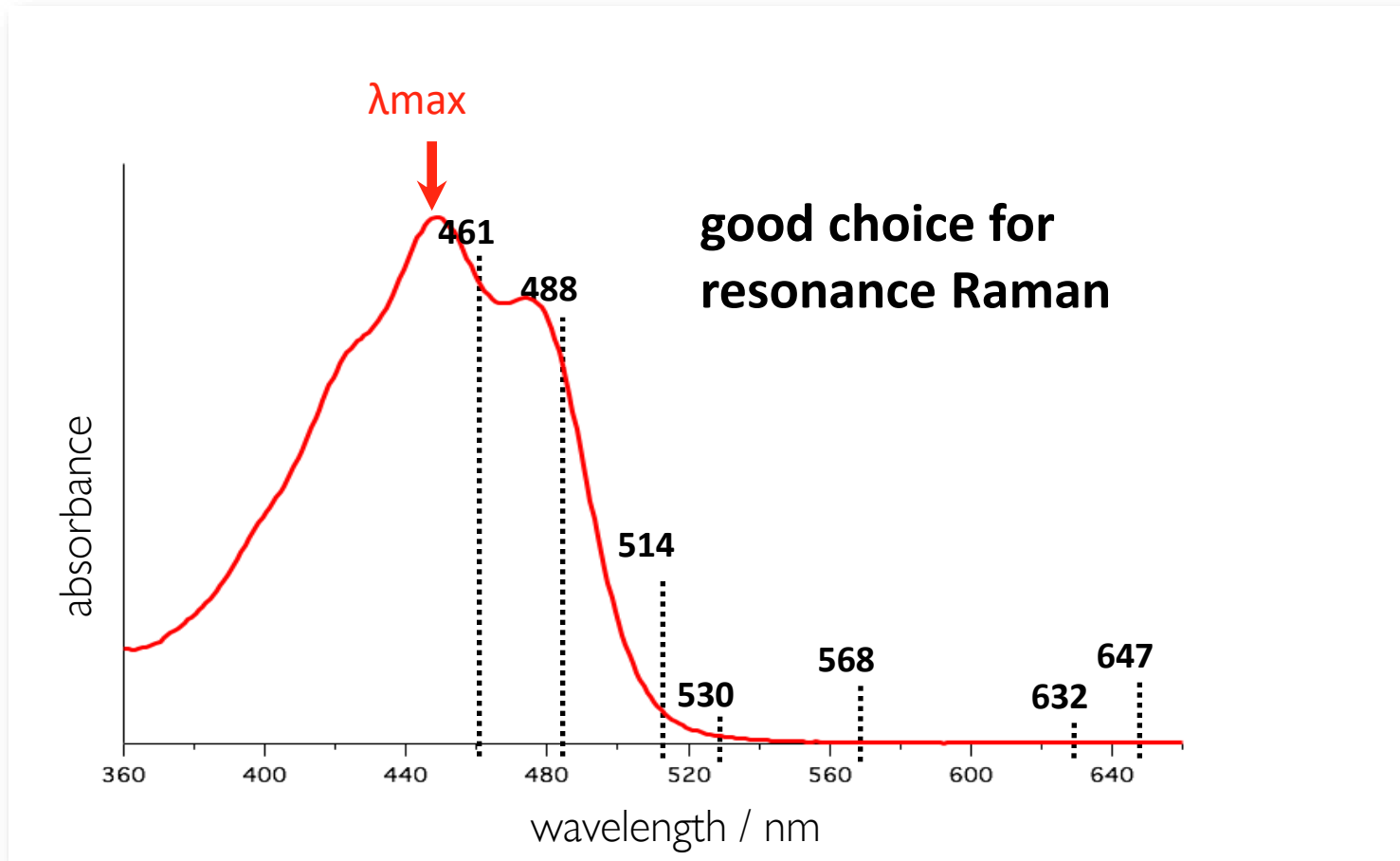
Cell Membrane

Thylakoid Membrane

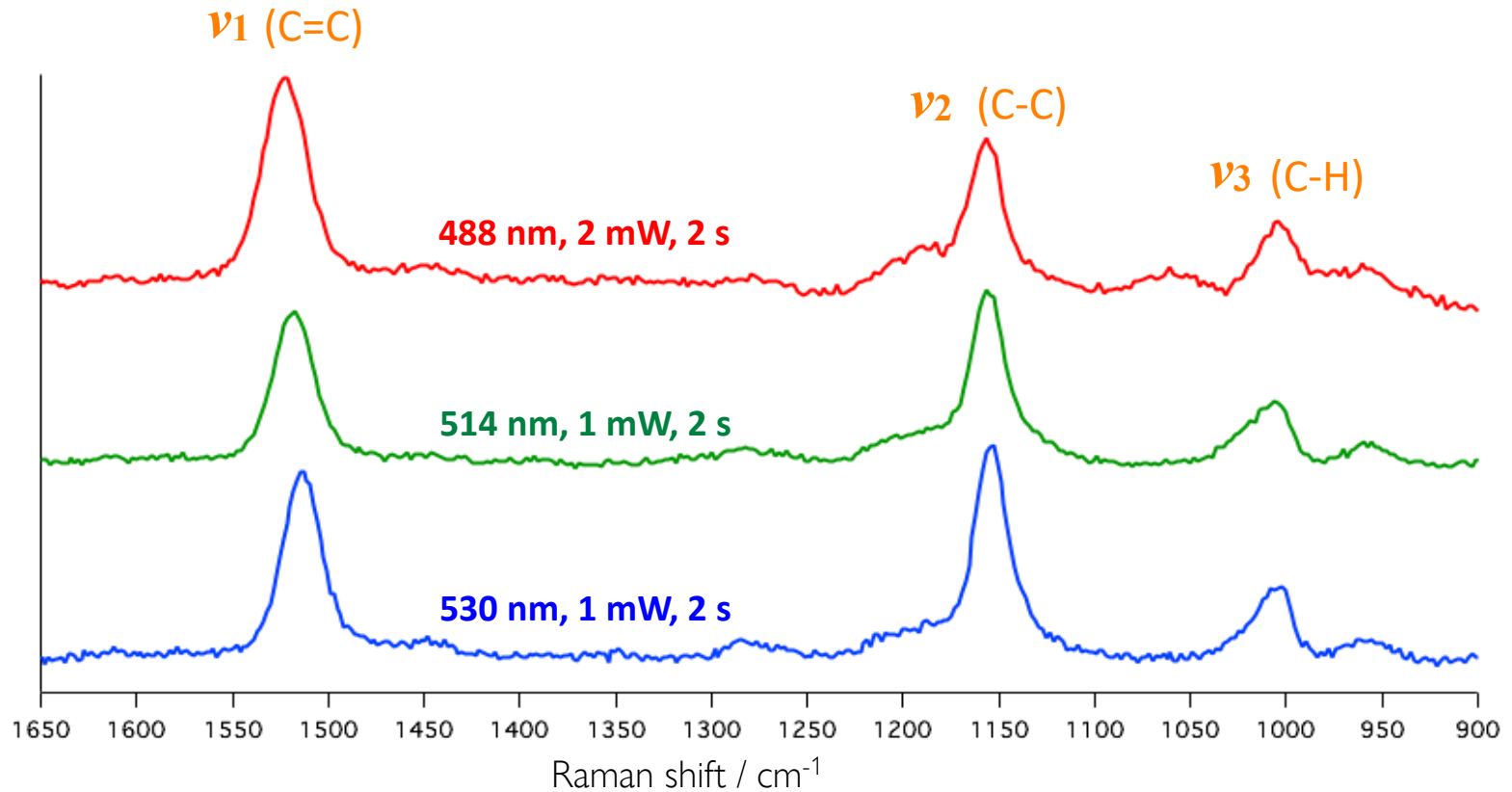




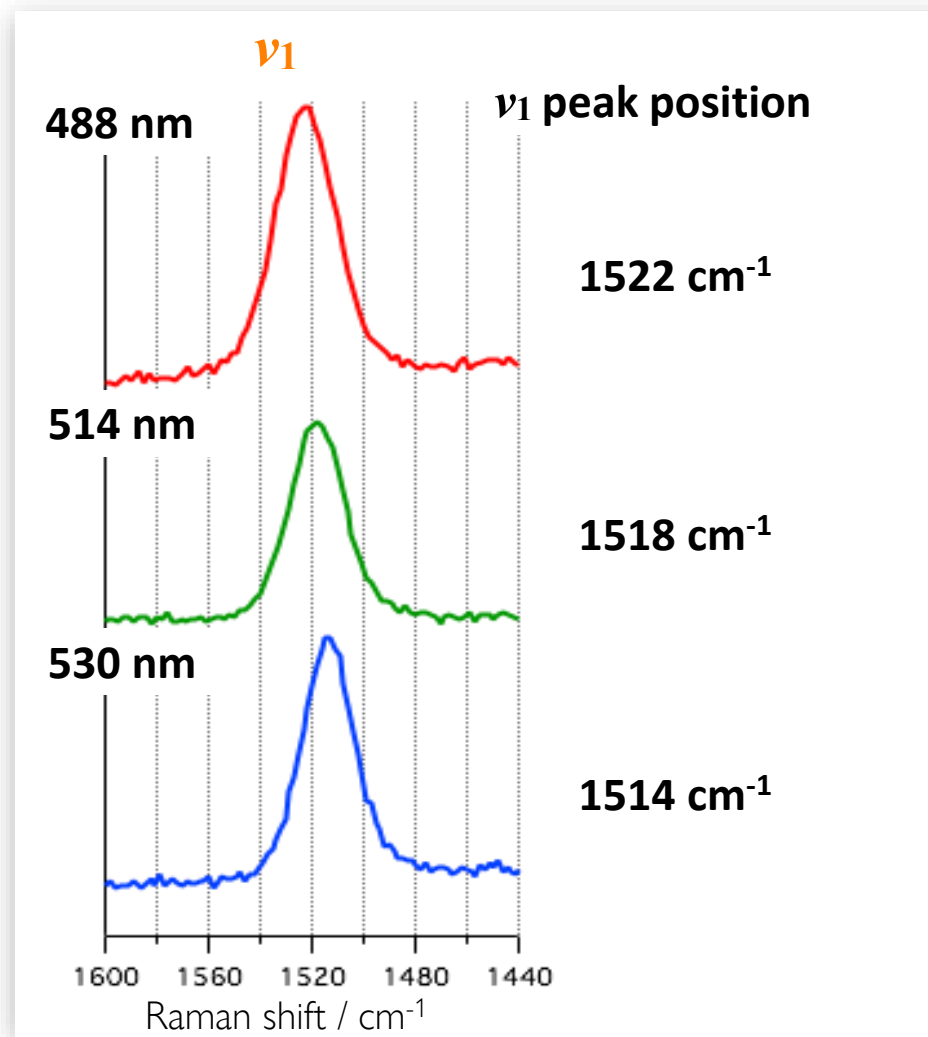
Absorption Spectra of β -carotene / cyclohexane (8 mg/L)



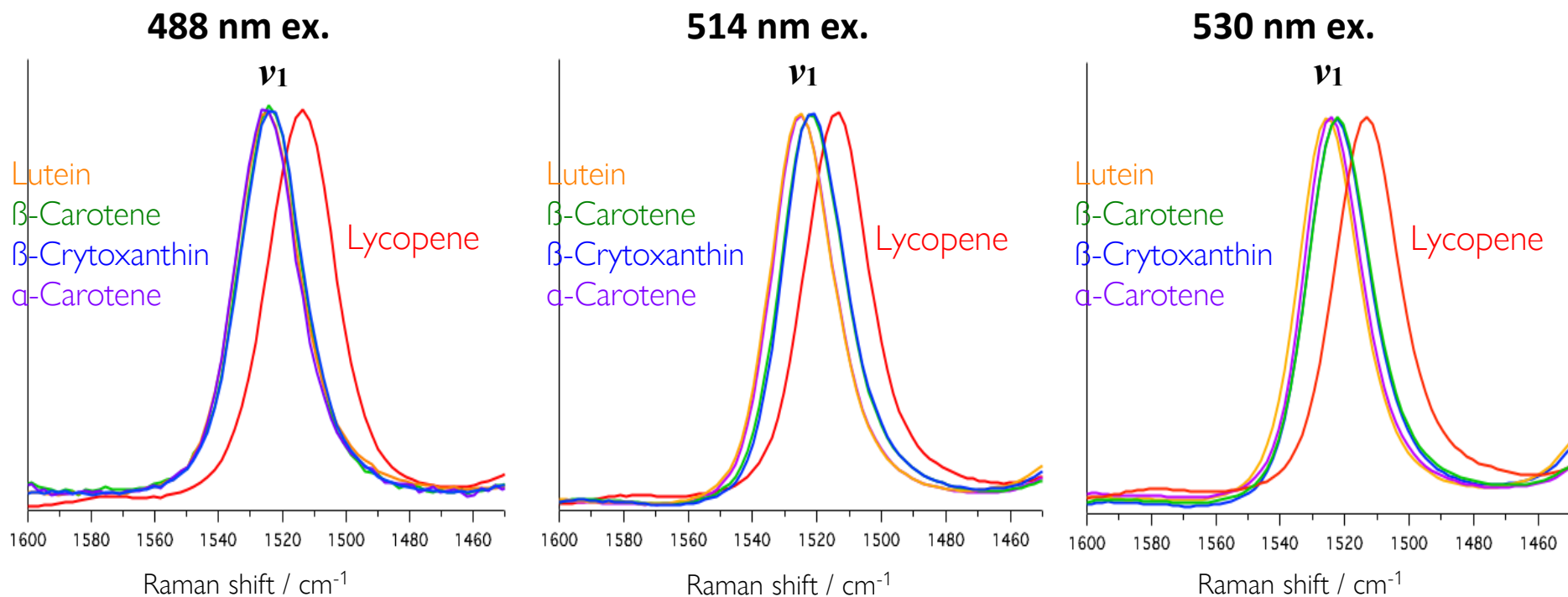
Raman Spectra of Serum with Different Excitation Wavelength



Raman Spectra of Serum with Different Excitation Wavelength

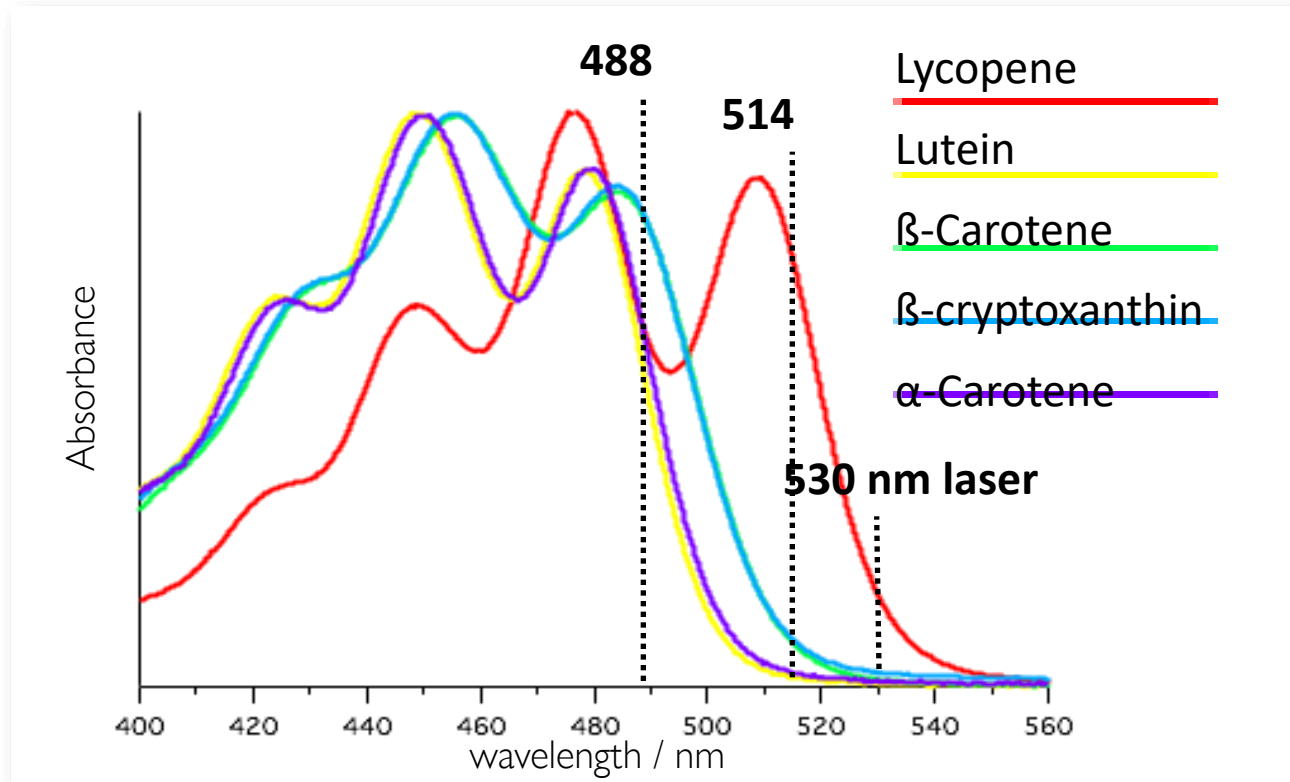


Raman Spectra of Carotenoids



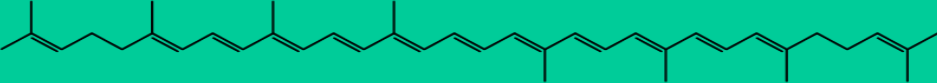
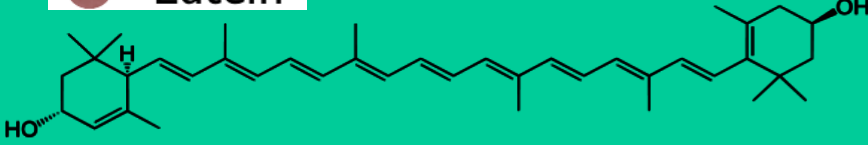
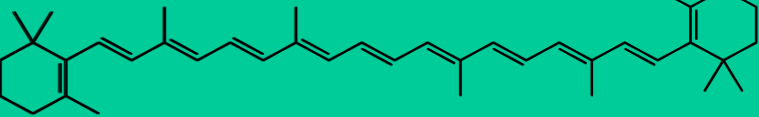
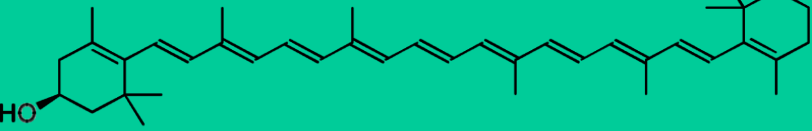

Lutein, β -Carotene, β -Crytoxanthin and α -Carotene have very similar ν_1 peak position, apart from Lycopene.

Absorption Spectra of Carotenoids



Lutein, α -Carotene, β -Crytoxanthin and β -Carotene have very similar absorption characteristics, apart from Lycopene.

Two Groups of Carotenoids in Serum

	λ_{\max} (nm)	ν_1 (cm^{-1})
 <p>Lycopene</p>	476.5	1512.8
 <p>Lutein</p>	449.0	1524.4
 <p>β-Carotene</p>	455.8	1523.7
 <p>β-cryptoxanthin</p>	455.4	1523.3
 <p>α-Carotene</p>	450.1	1524.8

Component 1 : Lycopene

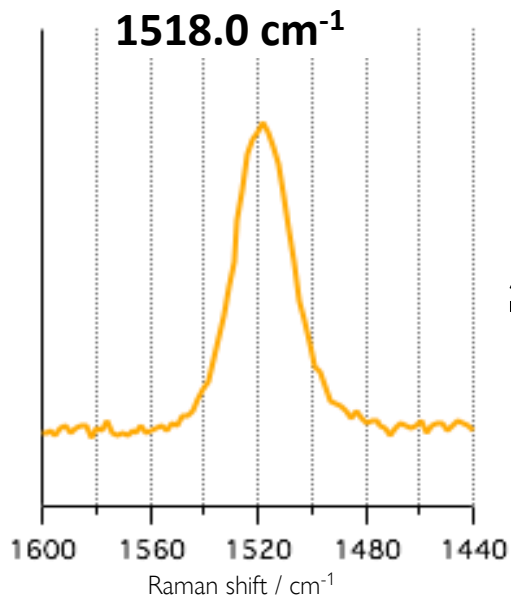
Component 2:

Represented by
β-Carotene

Fitting the Observed Band with Two Components

Serum Carotenoids

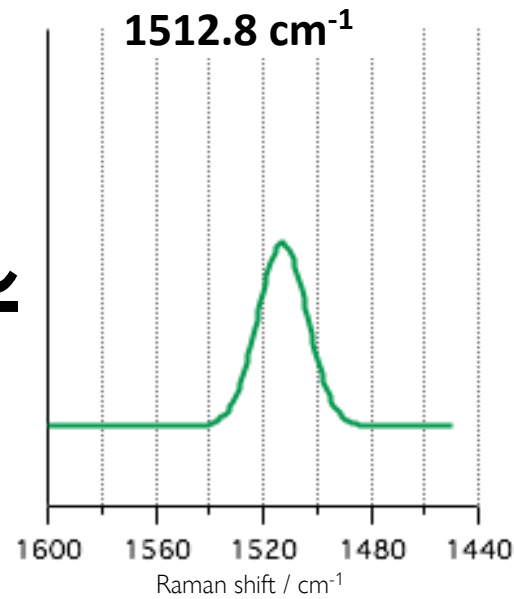
ν_1



\approx

Component 1

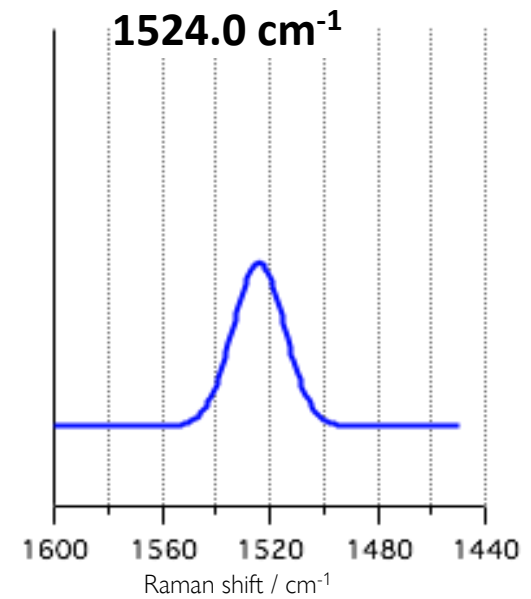
Lycopene



+

Component 2

β -Carotene



Proportion of Components Amplitude after Global Analysis

